

ECO-BOND GRAPHS

An Energy-Based Modeling and Simulation Framework for Complex Dynamic Systems

with a focus on Sustainability and Embodied Energy Flows

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ETH Zürich, Switzerland.

University of Buenos Aires & CIFASIS-CONICET, Argentina.

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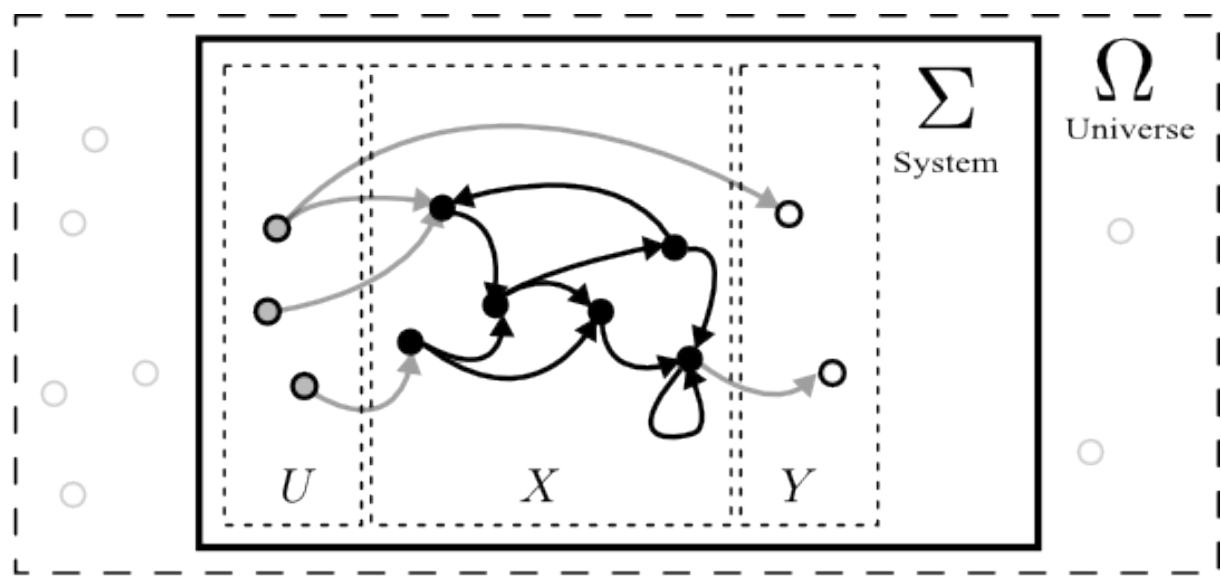
The 10th
International
Multidisciplinary
Modelling & Simulation
Multiconference



The 1st Int'l. Workshop on
Simulation for Energy, Sustainable
Development & Environment

- **Problem formulation**
 - Energy tracking & Complex Dynamics Systems
- **Possible approaches**
- **Our approach**
 - Networked Complex Processes
 - 3-faceted representation of energy flows
- **The Bond Graph formalism**
- **The new Eco Bond Graphs**
 - Definition
 - Examples
 - Simulation results
- **Conclusions**

- **Complex Dynamics Systems**
 - Global scale socio-natural processes

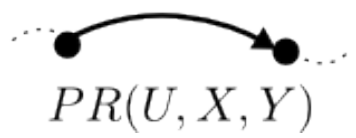


Linear System

$$\dot{X} = A.X + B.U$$

$$Y = C.X + D.U$$

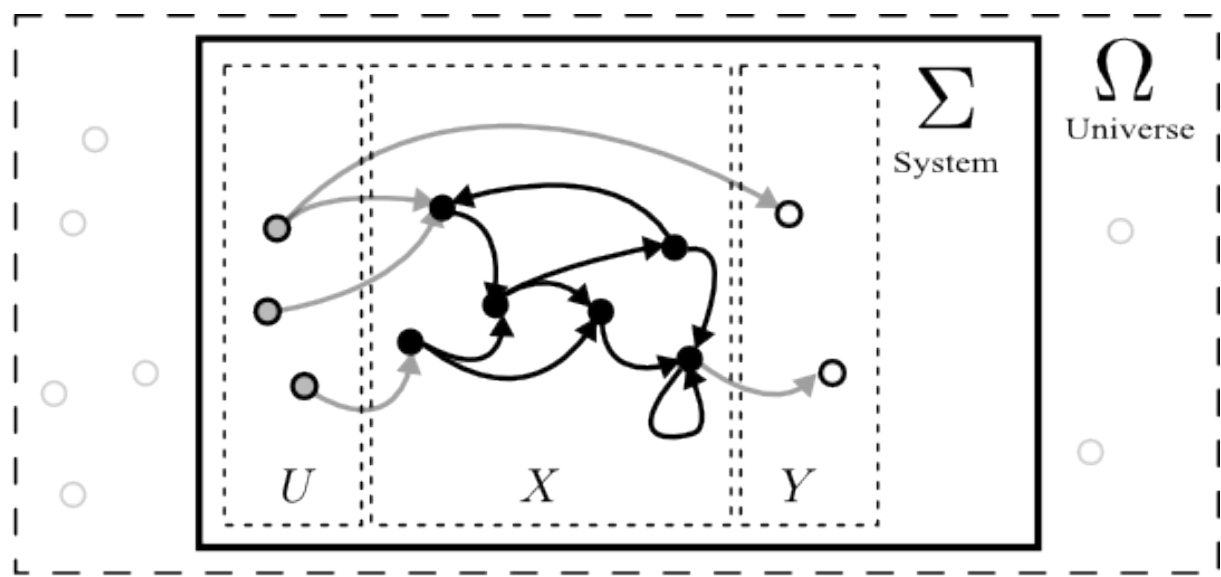
Complex System



$$\Sigma \subset \Omega$$

$$\Sigma = U \cup X \cup Y$$

- **Complex Dynamics Systems**
 - Global scale socio-natural processes
 - We live in a **nonlinear world**, mostly away from equilibrium

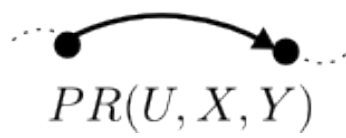


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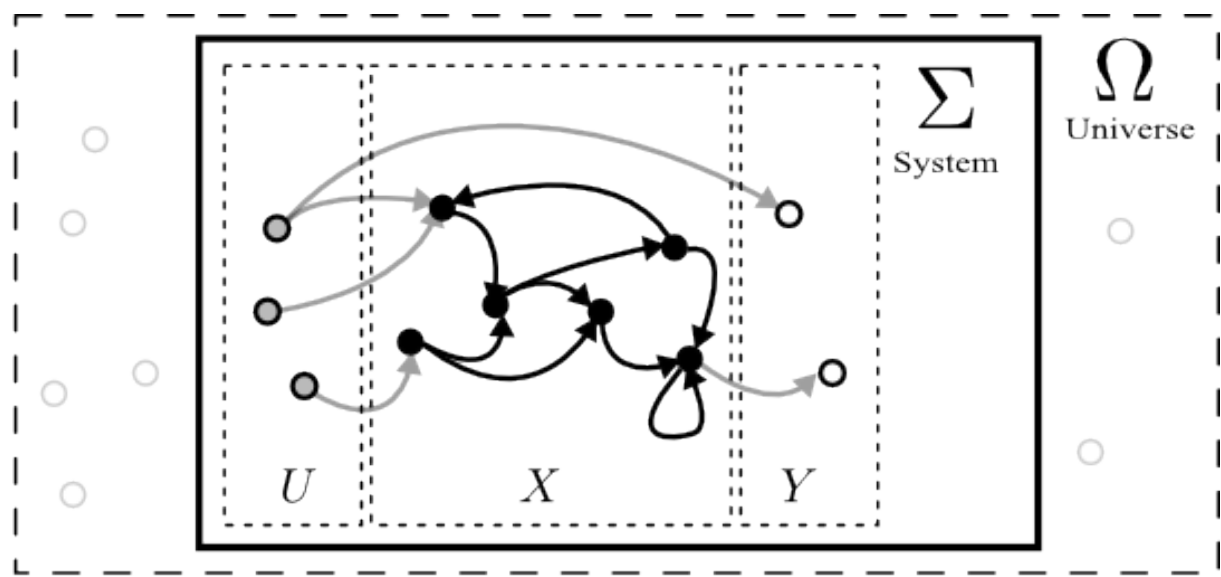
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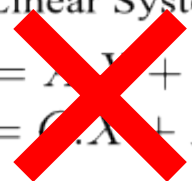
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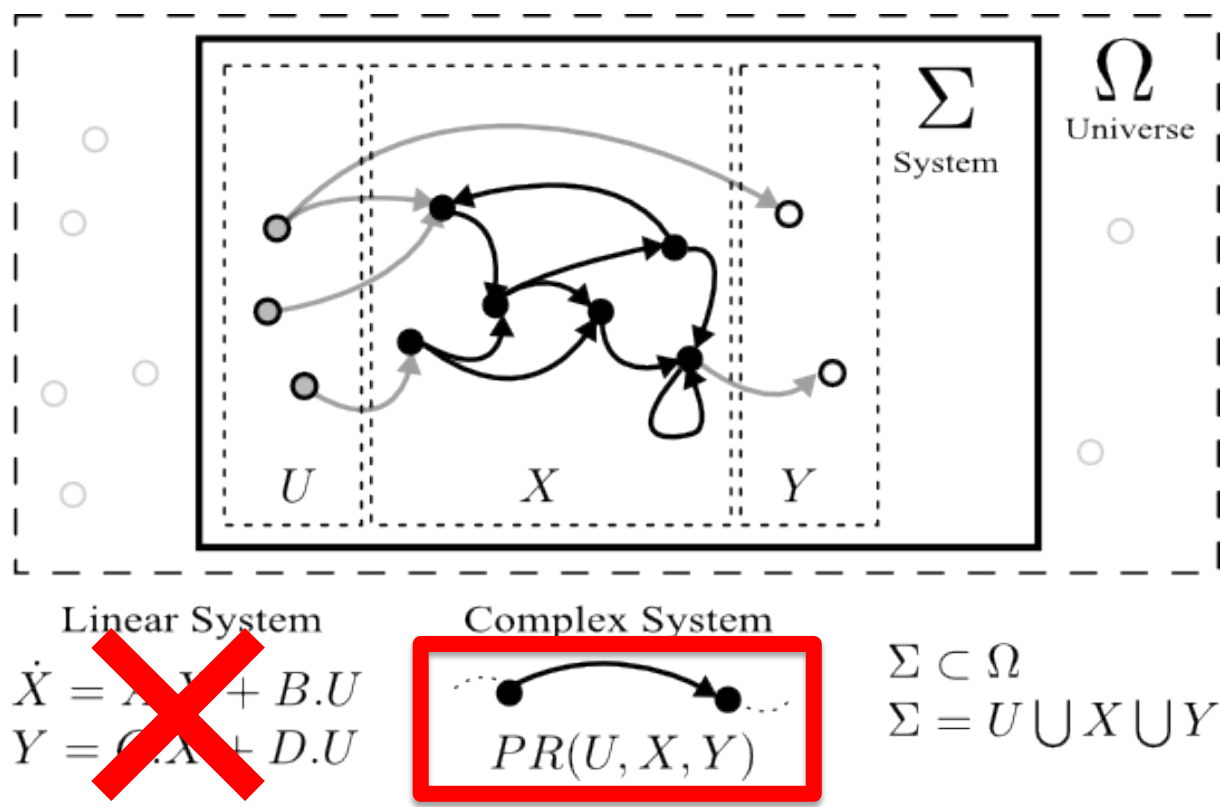
Complex System

$$PR(U, X, Y)$$

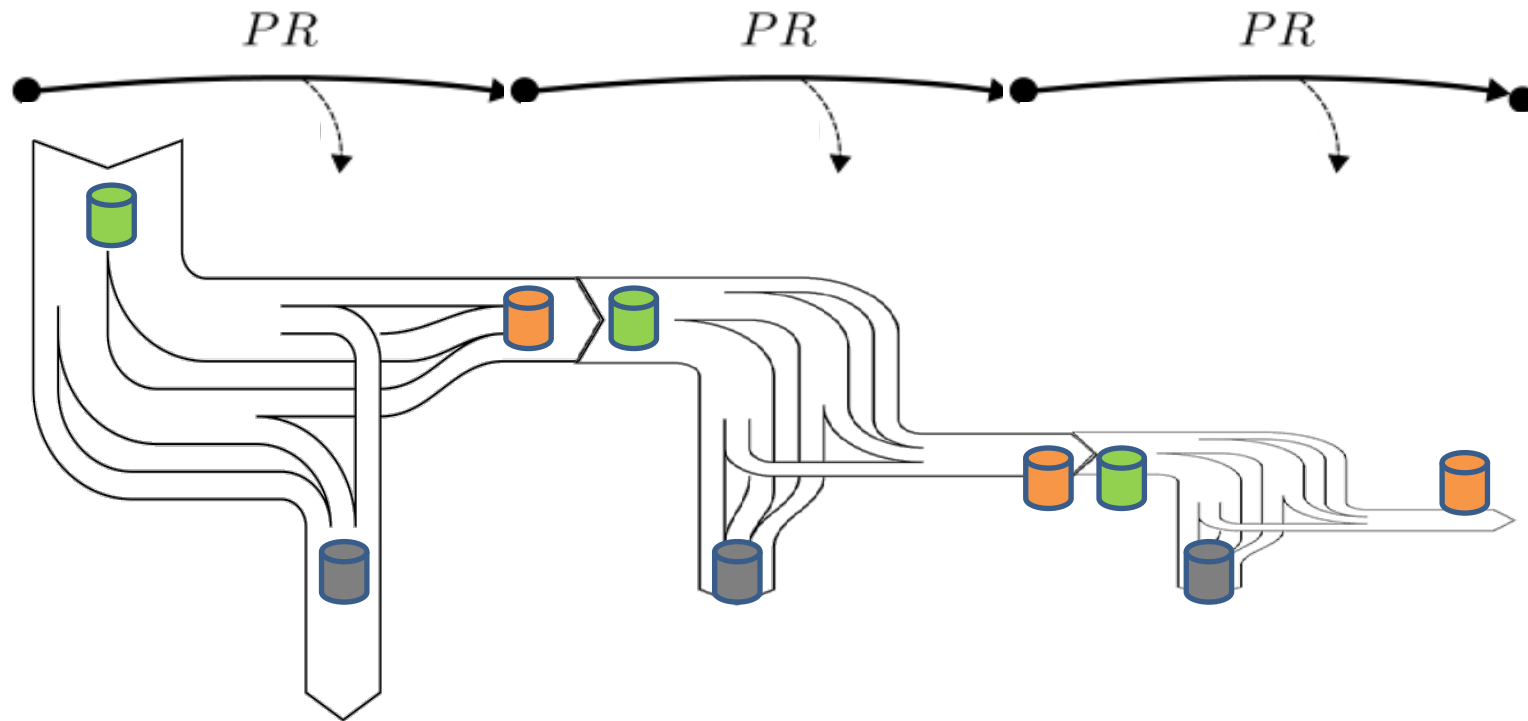
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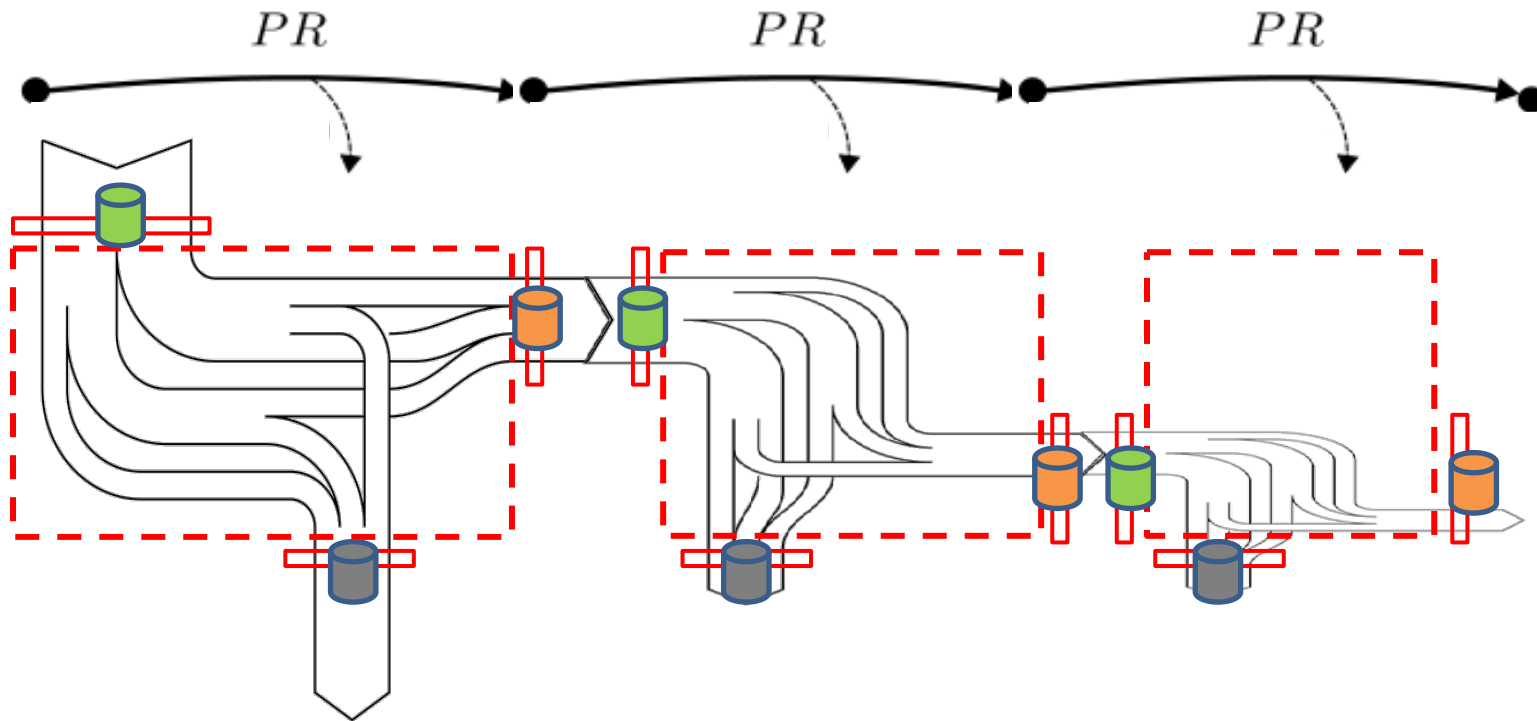
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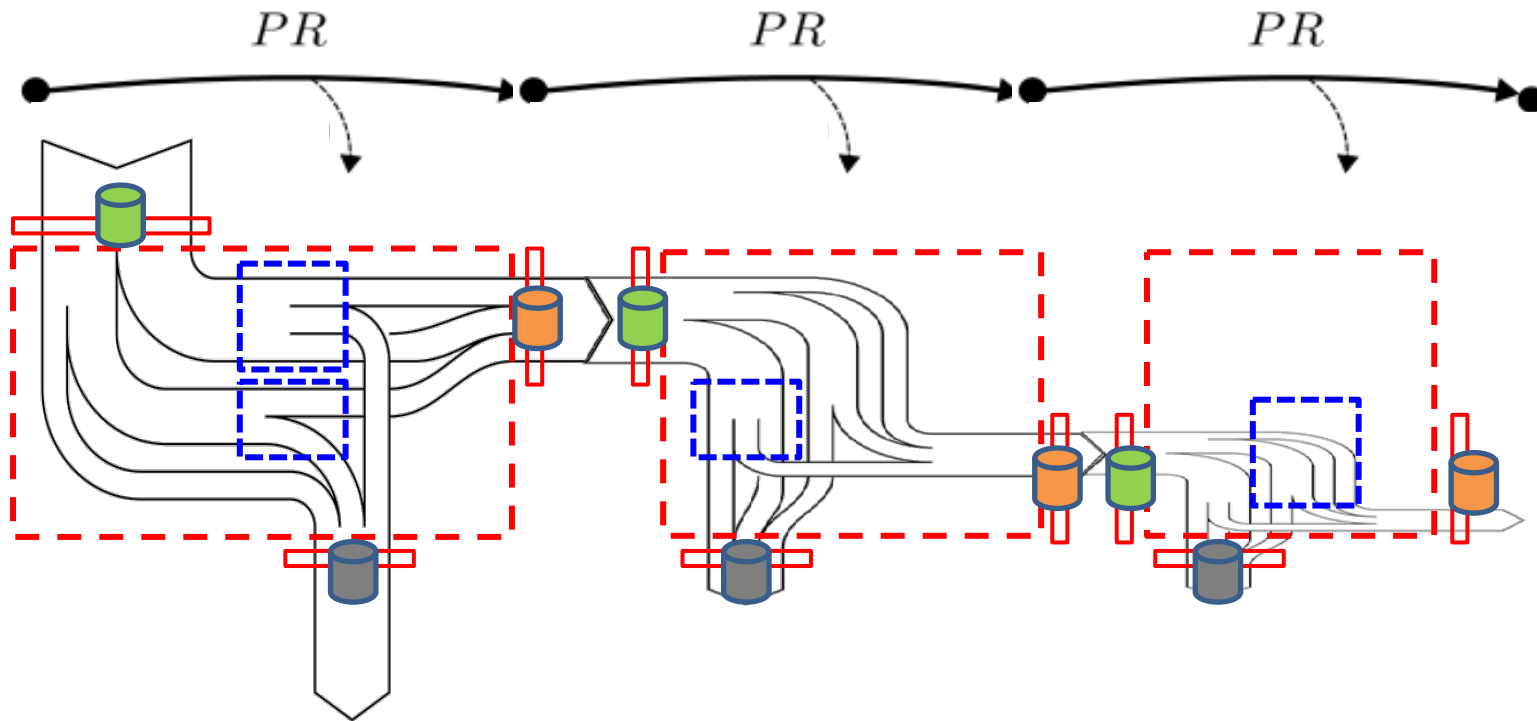
- Flows of Mass and Energy
 - Each process can abstract several internal sub processes.



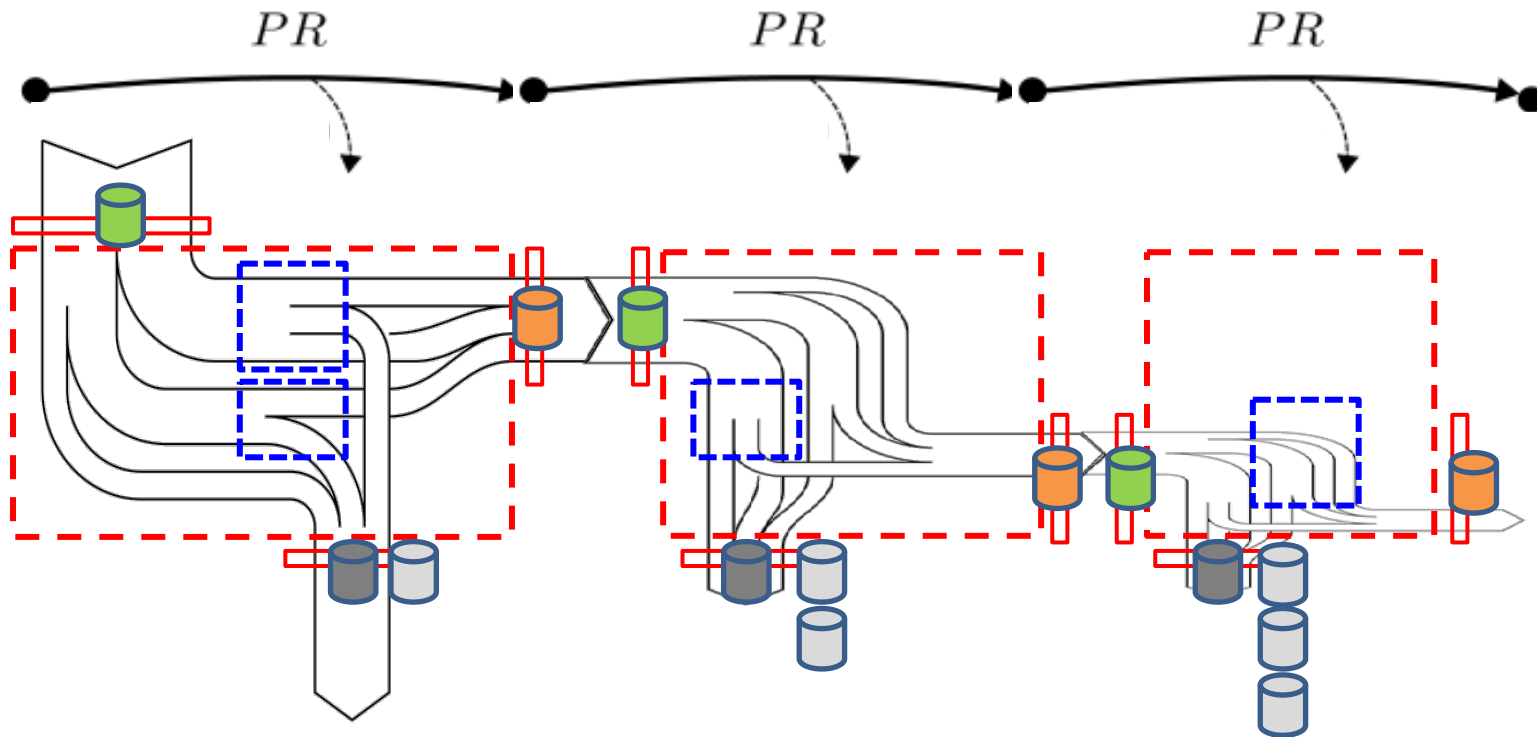
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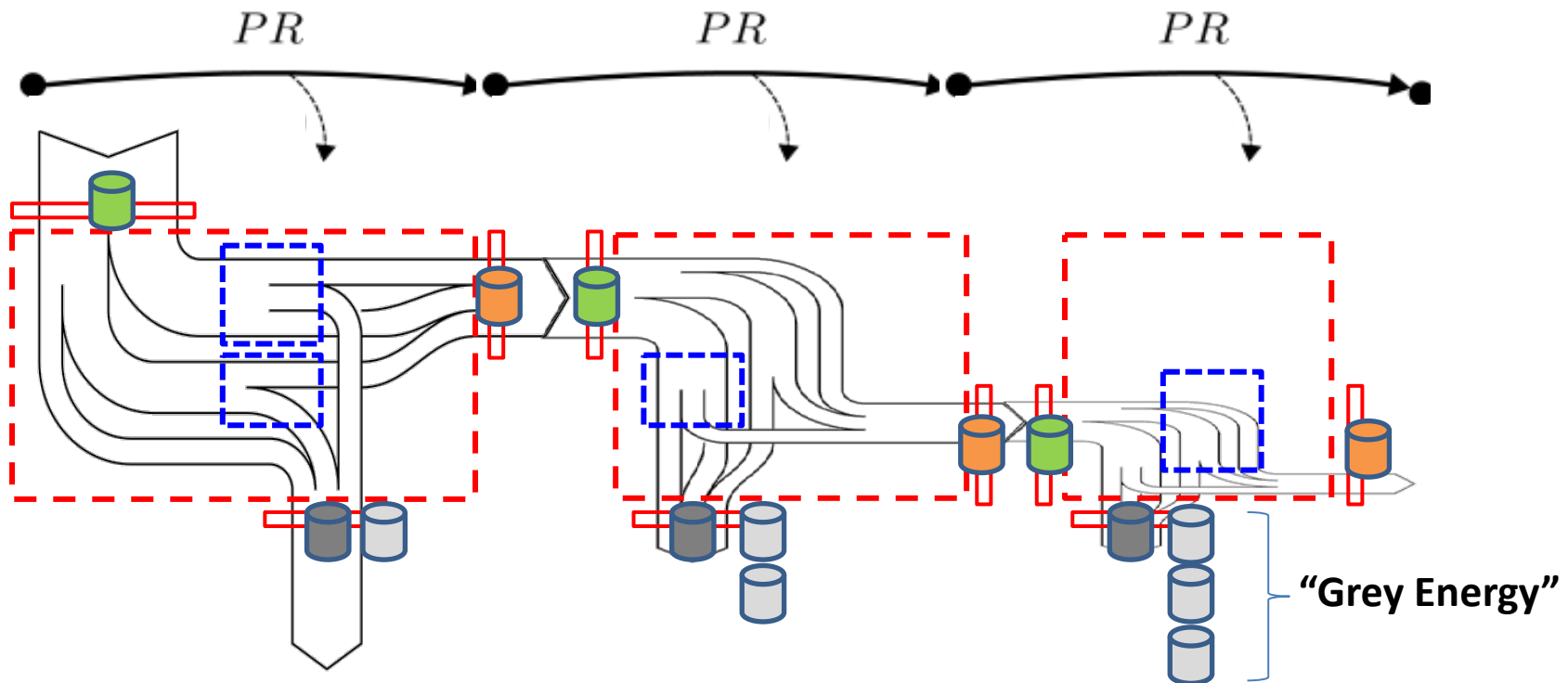
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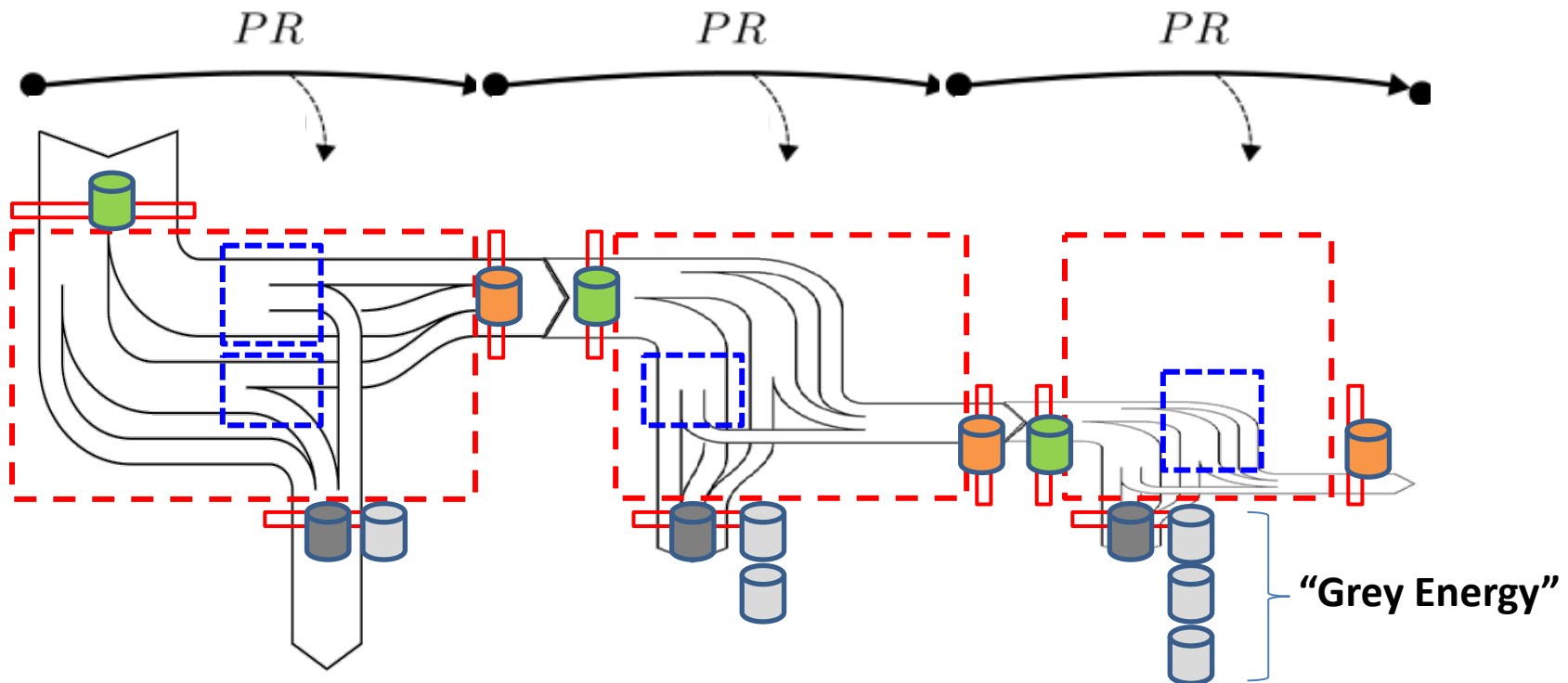
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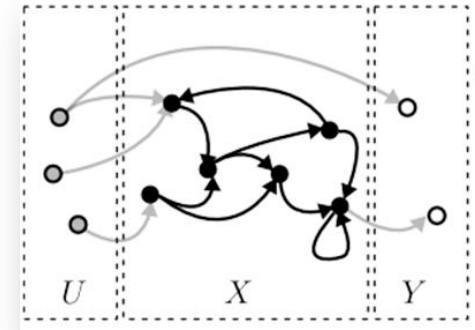


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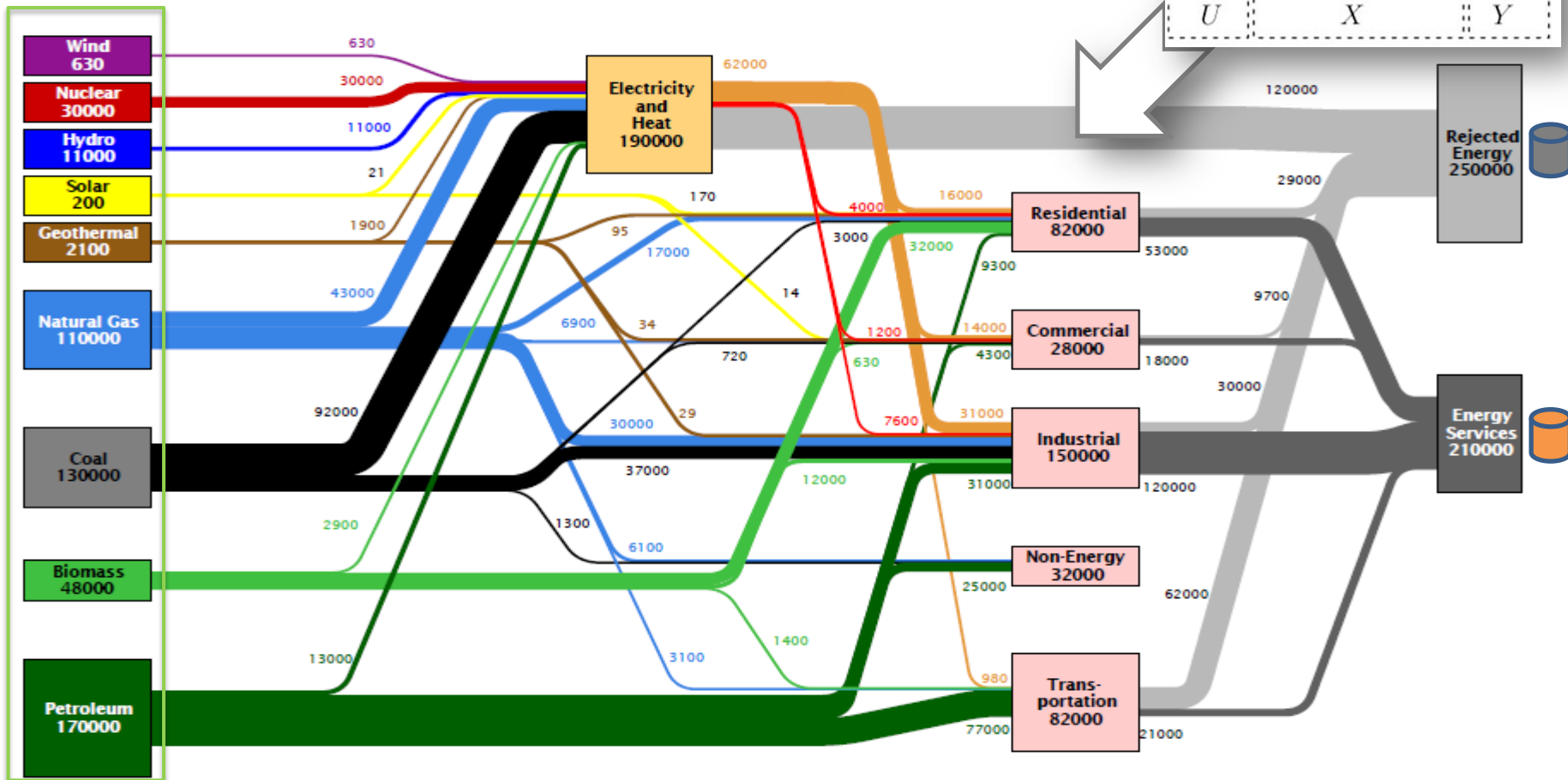
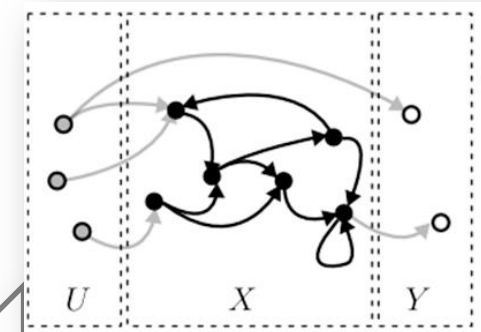
- We want to model systematically this type of systems
- Structural approach → Sustainability properties

- Sankey Diagrams
 - **Static** (snapshot-like) World Energy Flow.

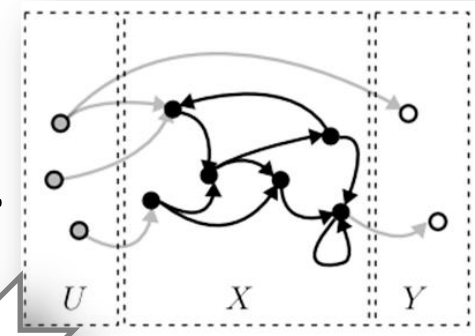


- Sankey Diagrams

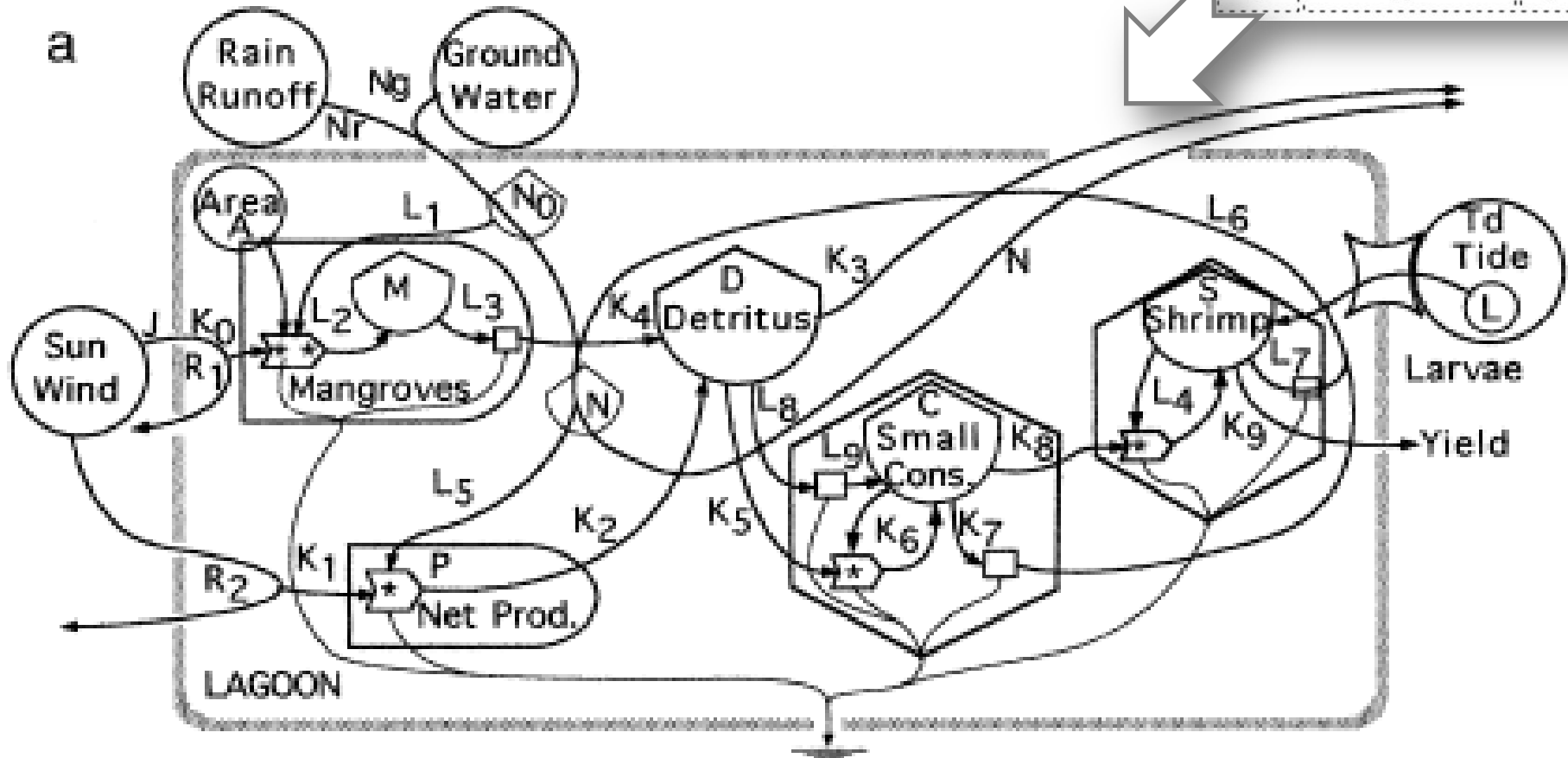
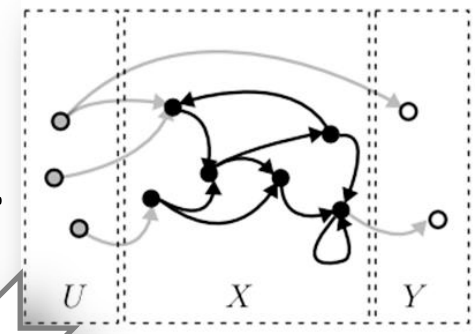
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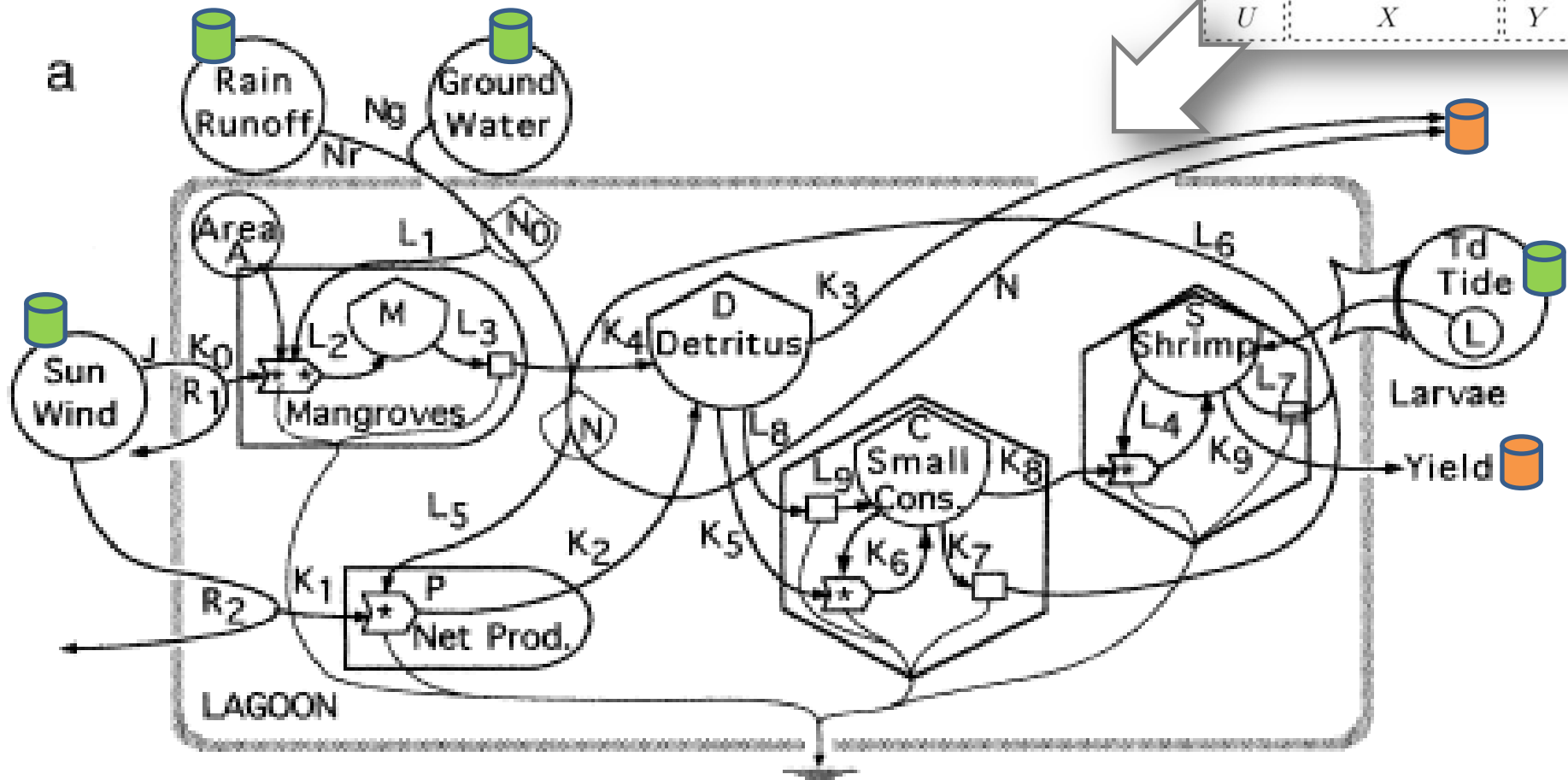
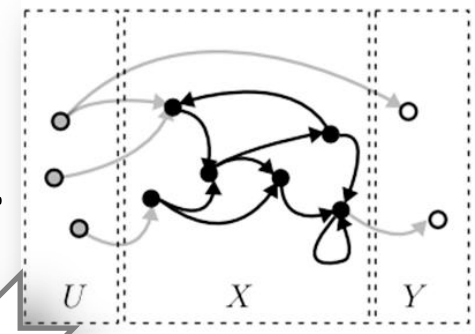
- Energy System Language (H.T. Odum)
 - Account for **dynamics** → Differential Eqns.



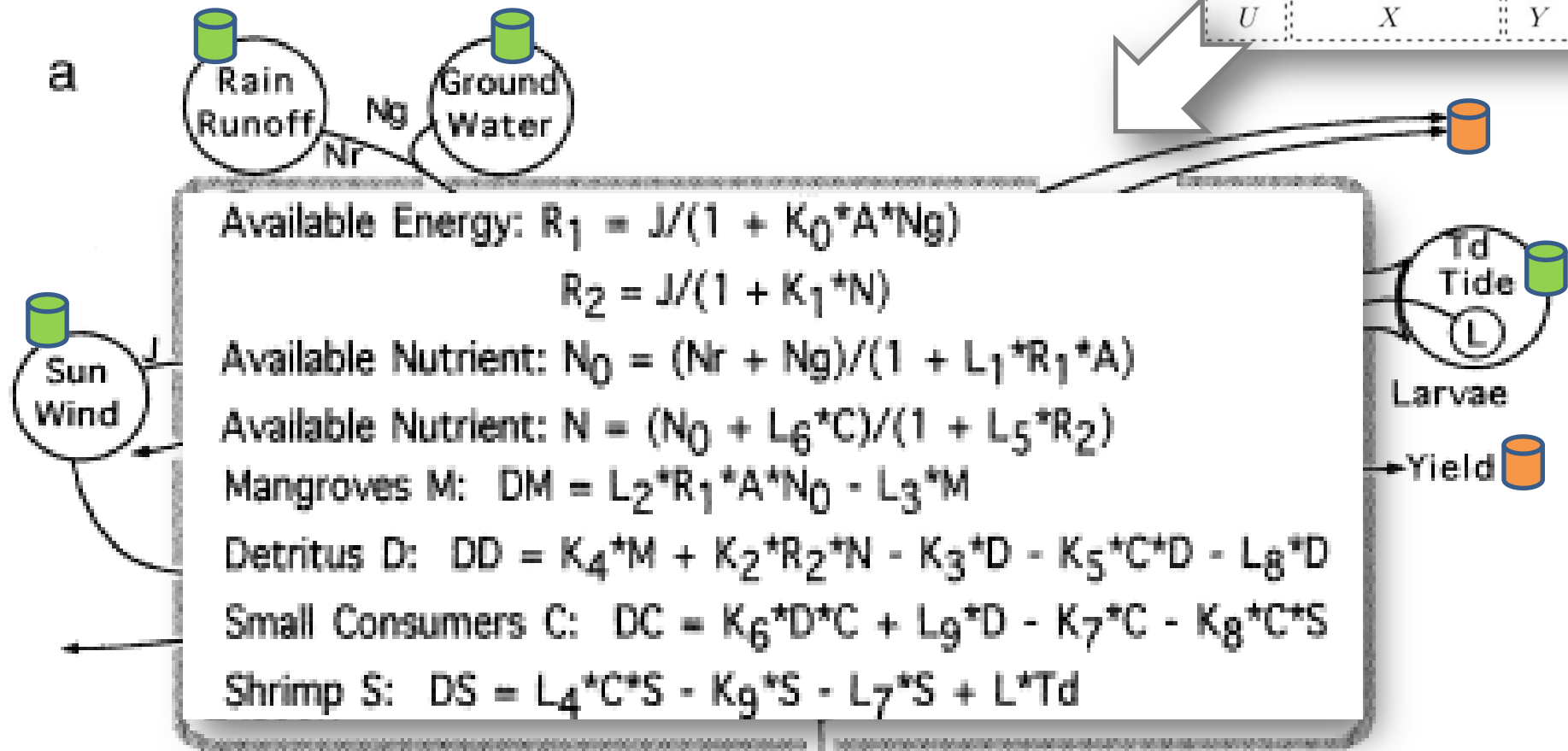
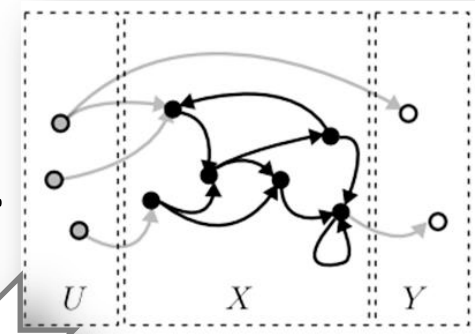
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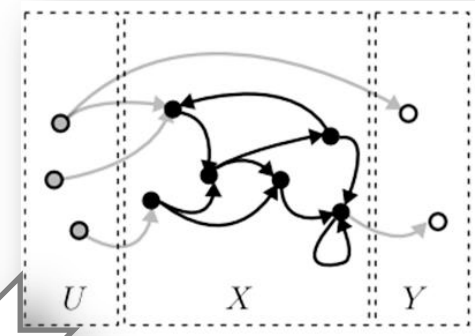


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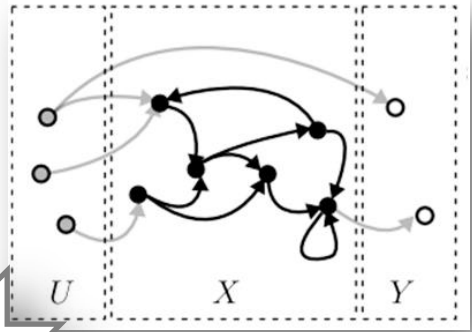
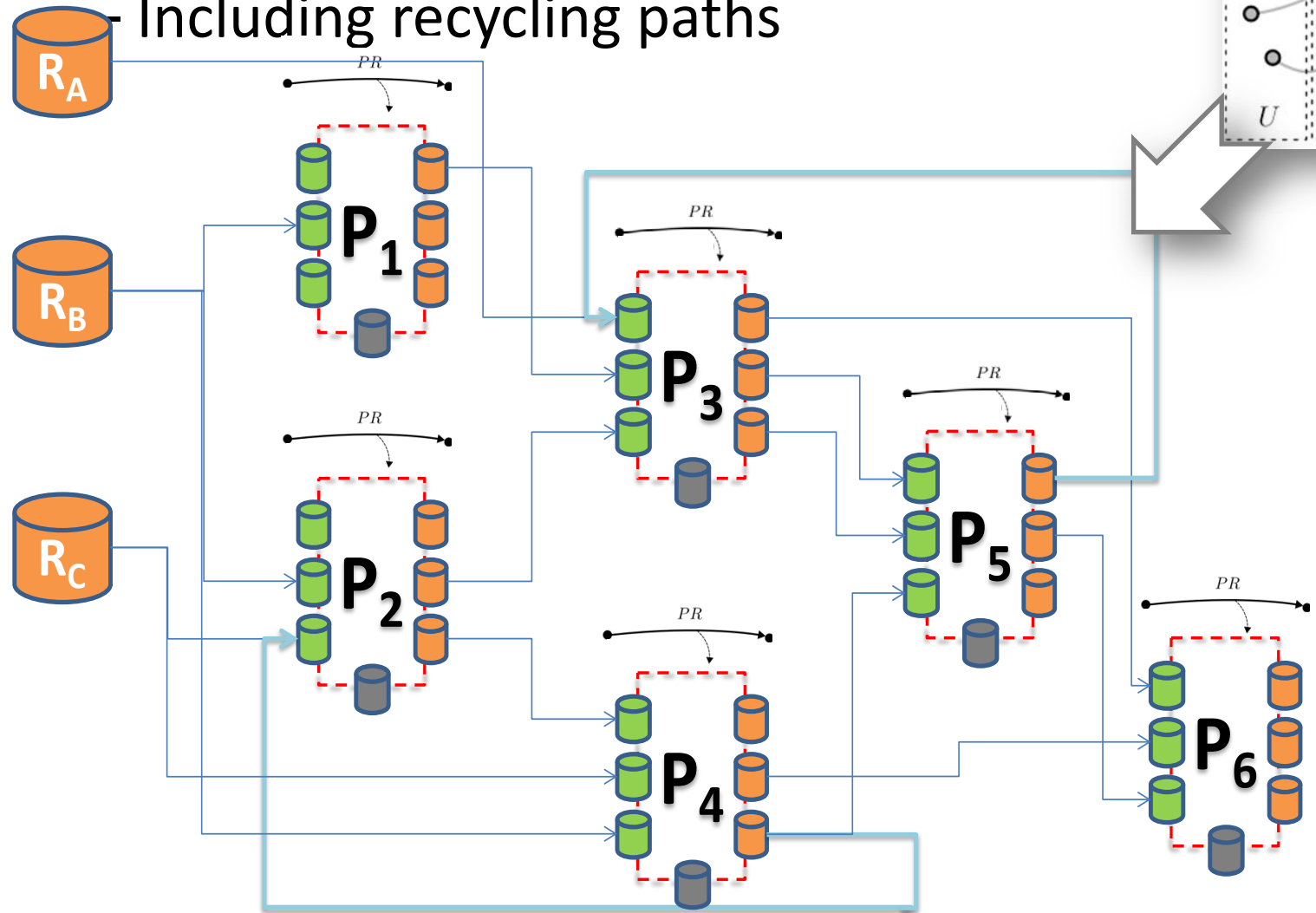
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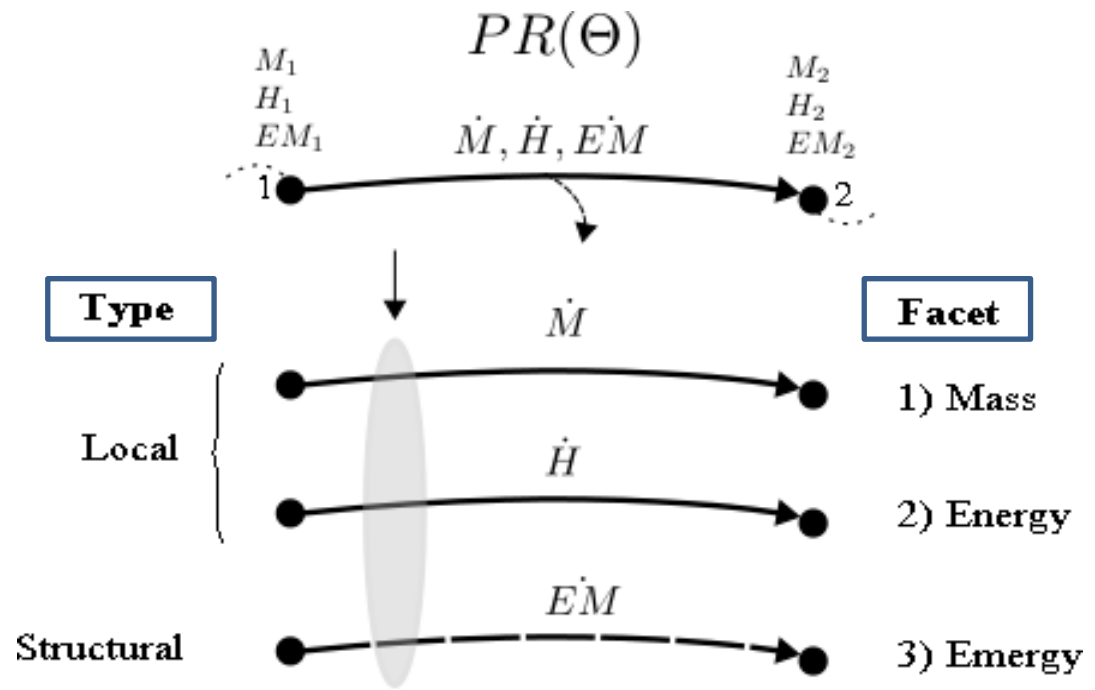


- Multi Input/Multi Output Processes

Including recycling paths



- 3-Faceted representation

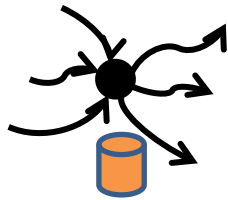


- 3-Faceted representation

Balance: Mass and Energy

$$\dot{M}_i = \sum \dot{M}_{i\text{in}} - \dot{M}_{i\text{out}}$$

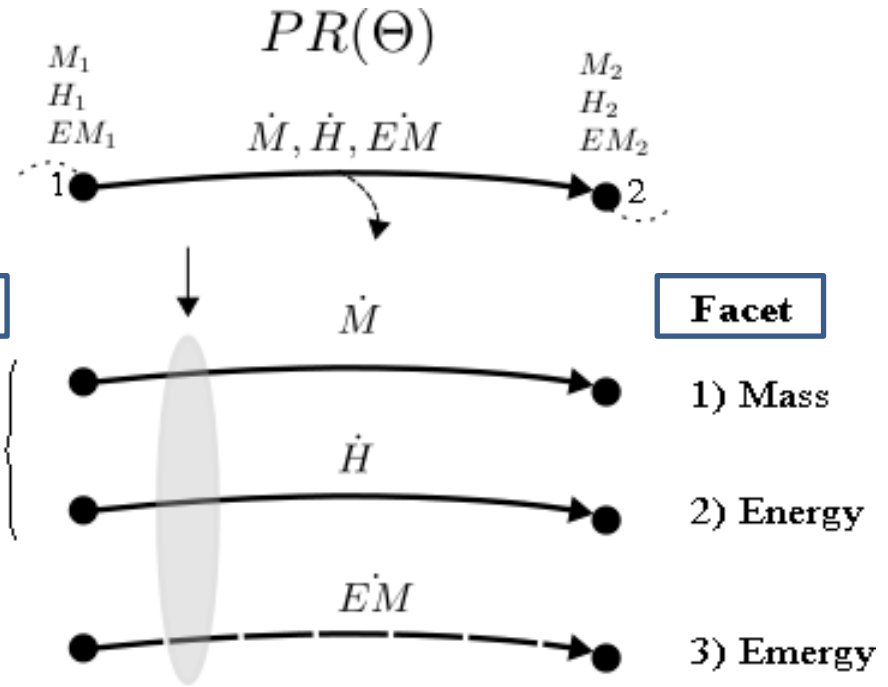
$$H_i = h_i \cdot M_i$$



Type

Local

Structural

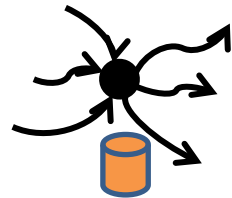


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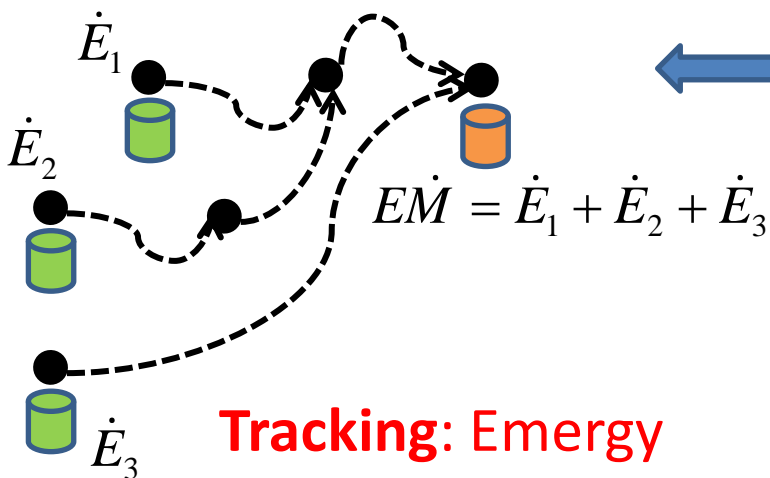


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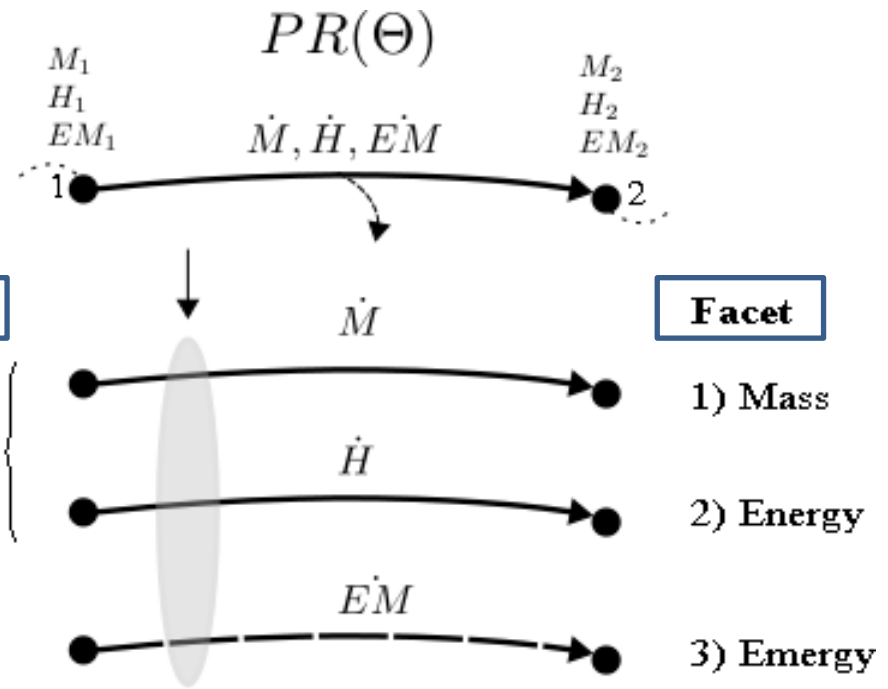
Local



Structural



Tracking: Energy

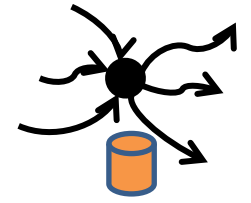


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Balance: Mass and Energy

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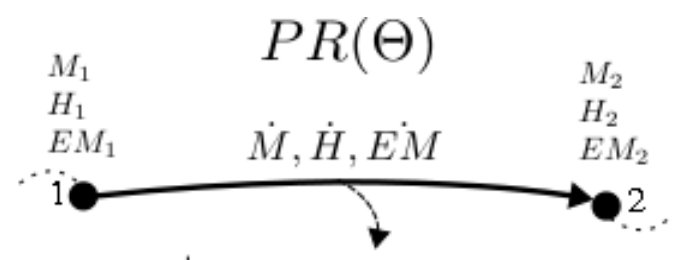
Facet

1) Mass

2) Energy

3) Energy

Structural



\dot{M}

\dot{H}

\dot{EM}

At a Process

$$\dot{M} = f_M(M_1, M_2, \Theta)$$

$$\dot{H} = f_H(H_1, H_2, \Theta)$$

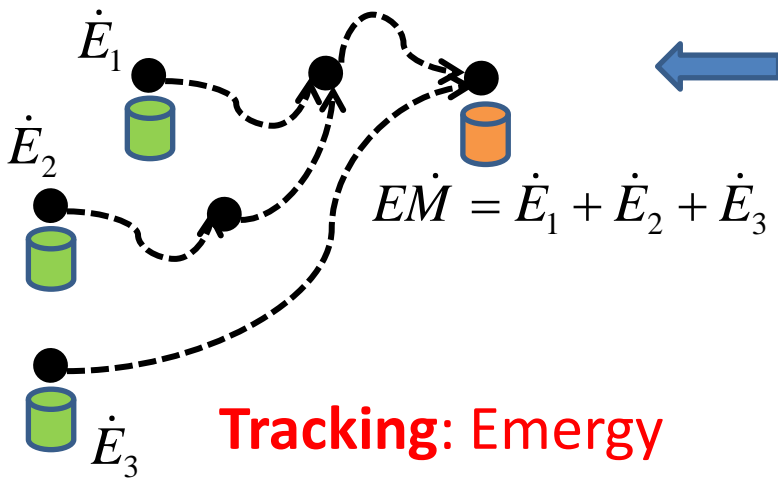
$$\dot{EM} = f_{EM}(EM_1, EM_2, \Theta)$$

At a Node

$$\dot{M}_i = \sum \dot{M}_{i\text{in}} - \dot{M}_{i\text{out}}$$

$$H_i = h_i \cdot M_i$$

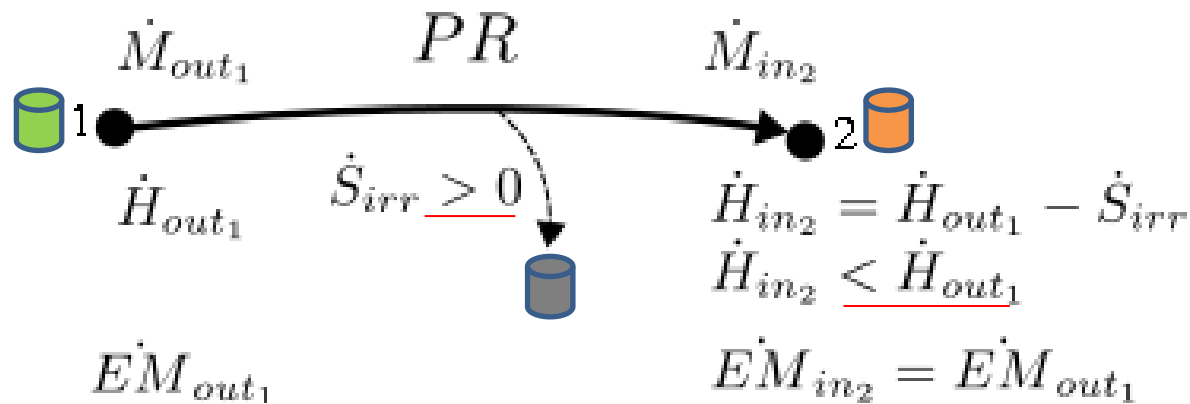
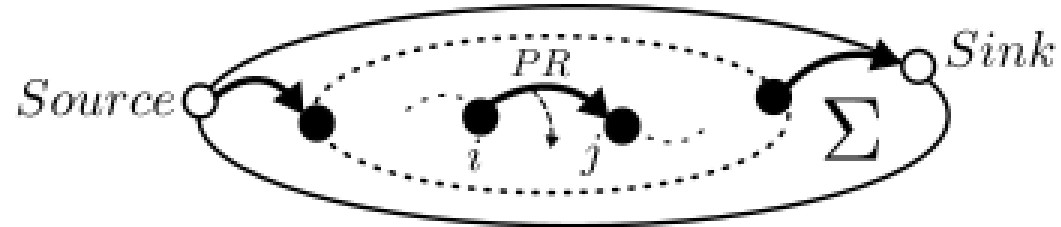
$$EM_i = em_i \cdot M_i$$



$$\dot{EM} = \dot{E}_1 + \dot{E}_2 + \dot{E}_3$$

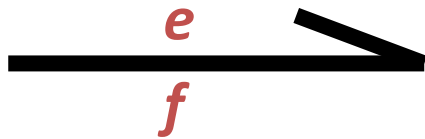
Tracking: Energy

- Minimum required formulation
 - To achieve the modeling goal systematically



- How do we **formalize and generalize** this structure ?

- Bondgraph is a graphical modeling technique
 - Rooted in the tracking of power [Joules/sec=Watt]
 - Represented by **effort variables (e)** and **flow variables (f)**

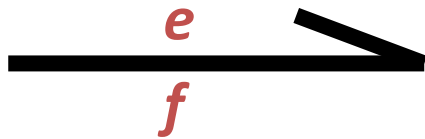


$$Power = e \cdot f$$

e: Effort

f: Flow

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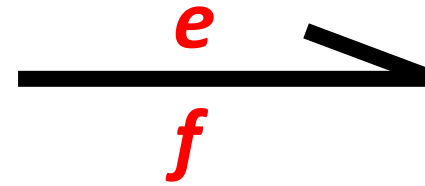
$$Power = e \cdot f$$

e: **Effort**

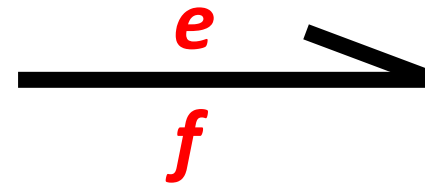
f: **Flow**

- **Goal:**
 - **Sound** physical modeling of generalized flows of energy
 - **Self checking** capabilities for thermodynamic **feasibility**
- **Strategy:**
 - Bondgraphic modeling of phenomenological processes
 - Including energy tracking capabilities

- **Bondgraph** is multi-energy domain

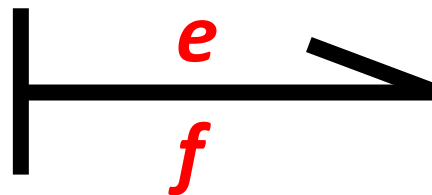


- **Bondgraph** is multi-energy domain

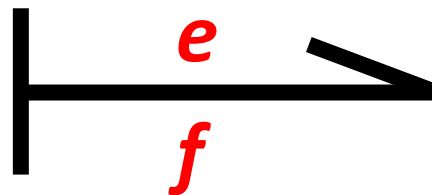


Energy Domain	Effort variable	Flow variable
Mechanical, translation	Force	Linear velocity
Mechanical, rotation	Torque	Angular velocity
Electrical	Electromotive force	Current
Magnetic	Magnetomotive force	Flux rate
Hydraulic	Pressure	Volumetric flow rate
Thermal	temperature	entropy flow rate

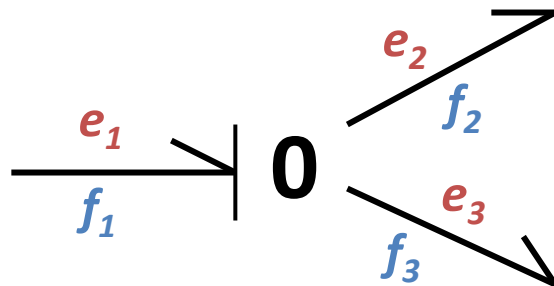
- As every bond defines two **separate variables**
 - The **effort e** and the **flow f**
 - **We need two equations** to compute values for these two variables
- It is **always possible** to compute **one of the two variables at each side of the bond.**



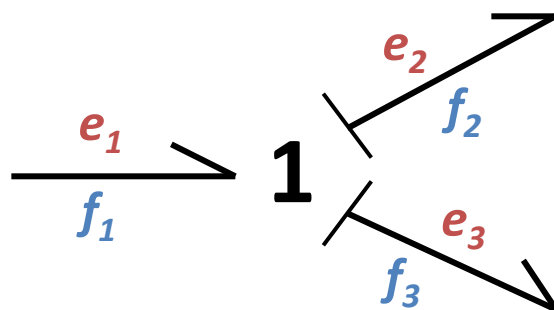
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 - The **effort e** and the **flow f**
 - **We need two equations** to compute values for these two variables
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- A **vertical bar** symbolizes the side where the **flow** is being computed.



- Local balances of energy

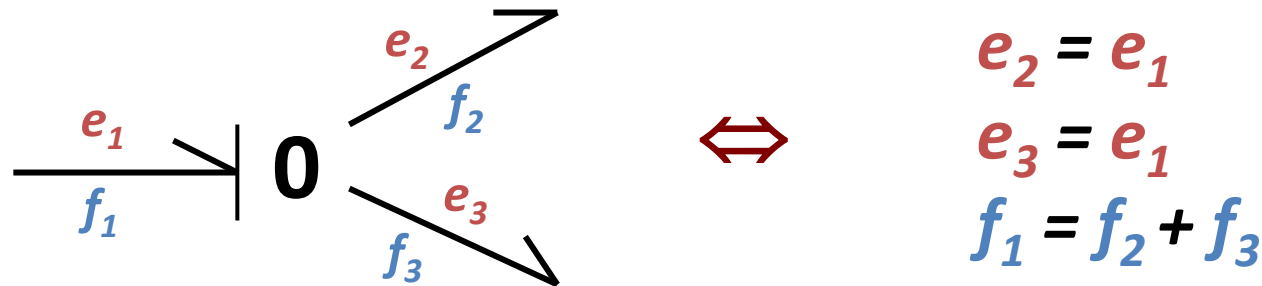


$$\begin{aligned} e_2 &= e_1 \\ e_3 &= e_1 \\ f_1 &= f_2 + f_3 \end{aligned}$$

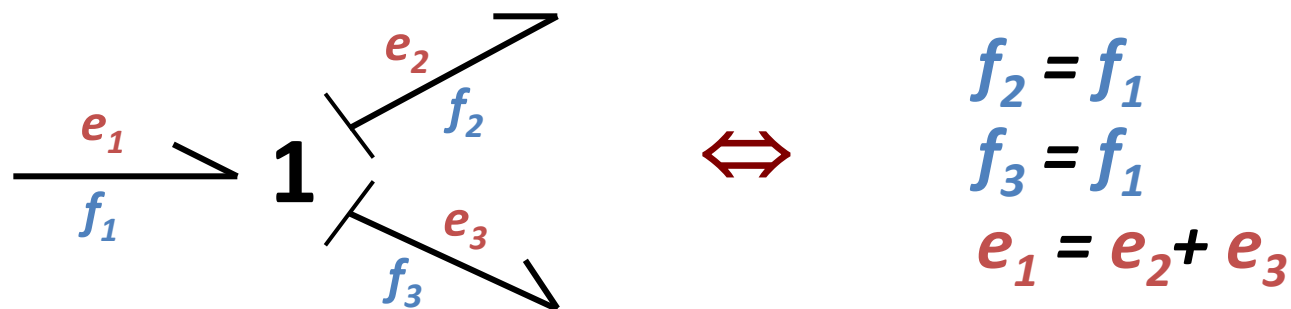


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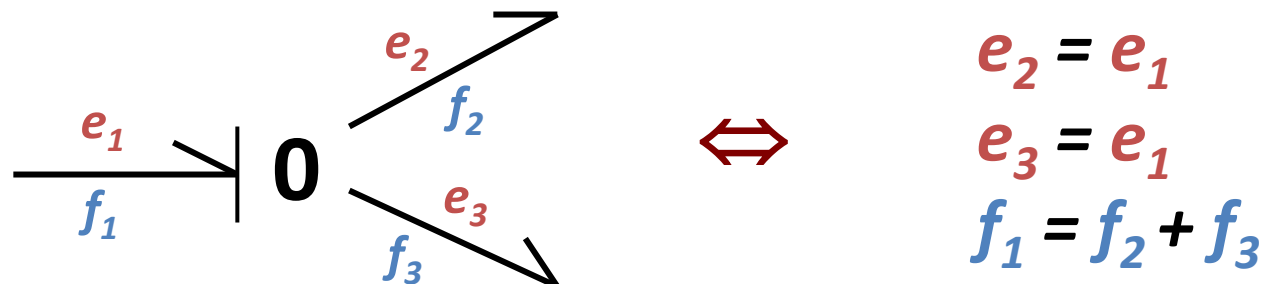
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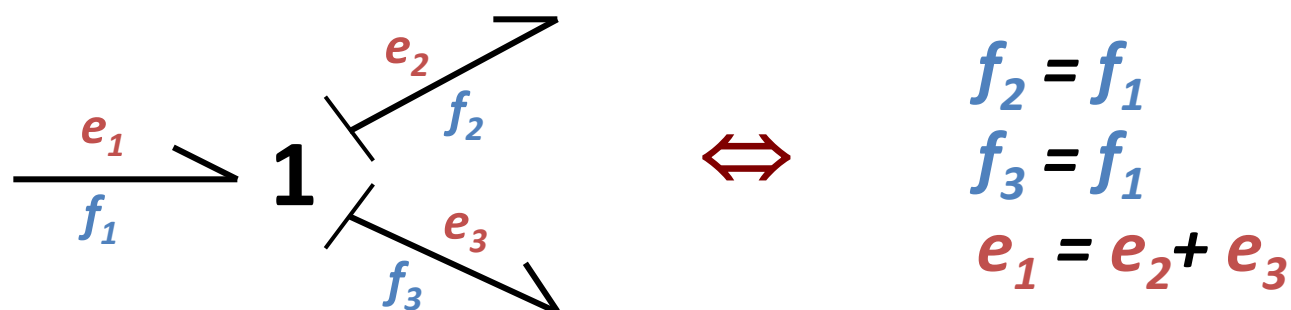
*Junctions of type **0** have only one flow equation, and therefore, they must have exactly one causality bar.*



- Local balances of energy



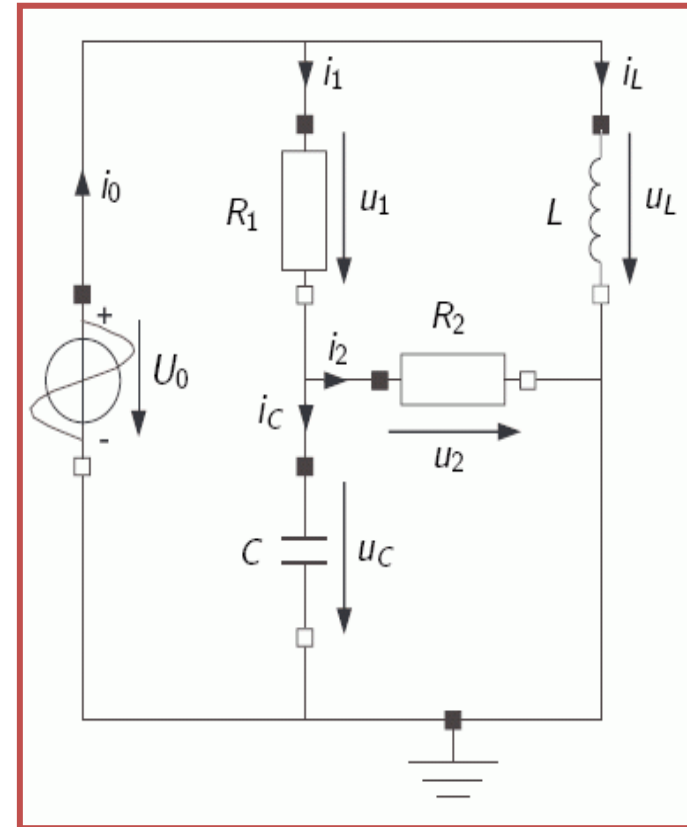
Junctions of type **0** have **only one flow equation**, and therefore, they must have exactly **one causality bar**.



Junctions of type **1** have **only one effort equation**, and therefore, they must have exactly **(n-1) causality bars**.

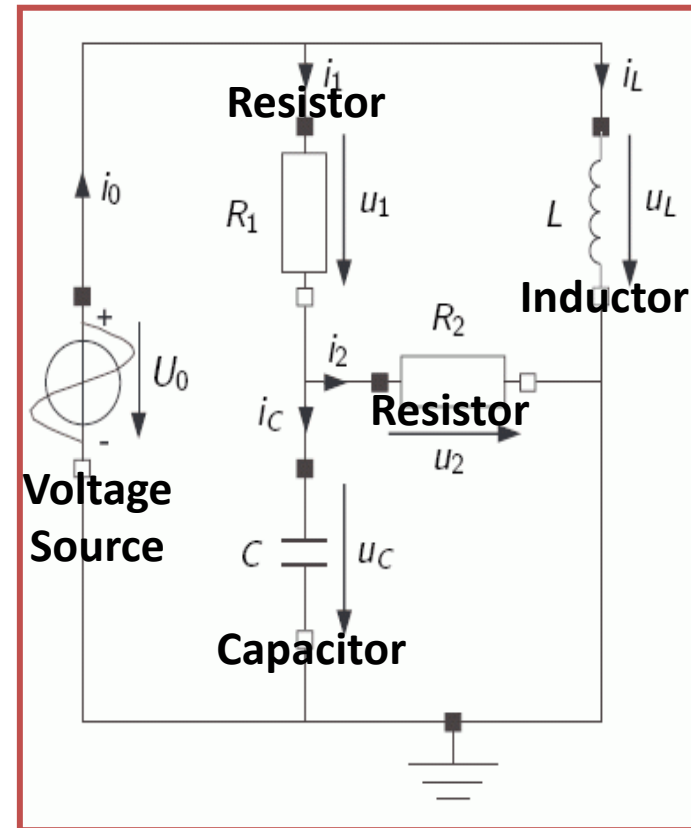
- An electrical energy domain model

Electrical Circuit



- An electrical energy domain model

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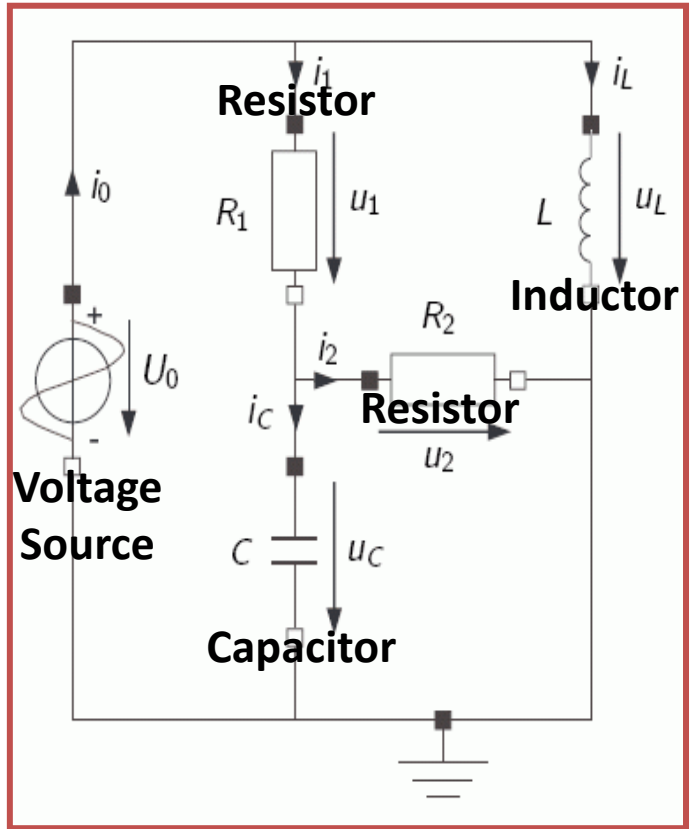
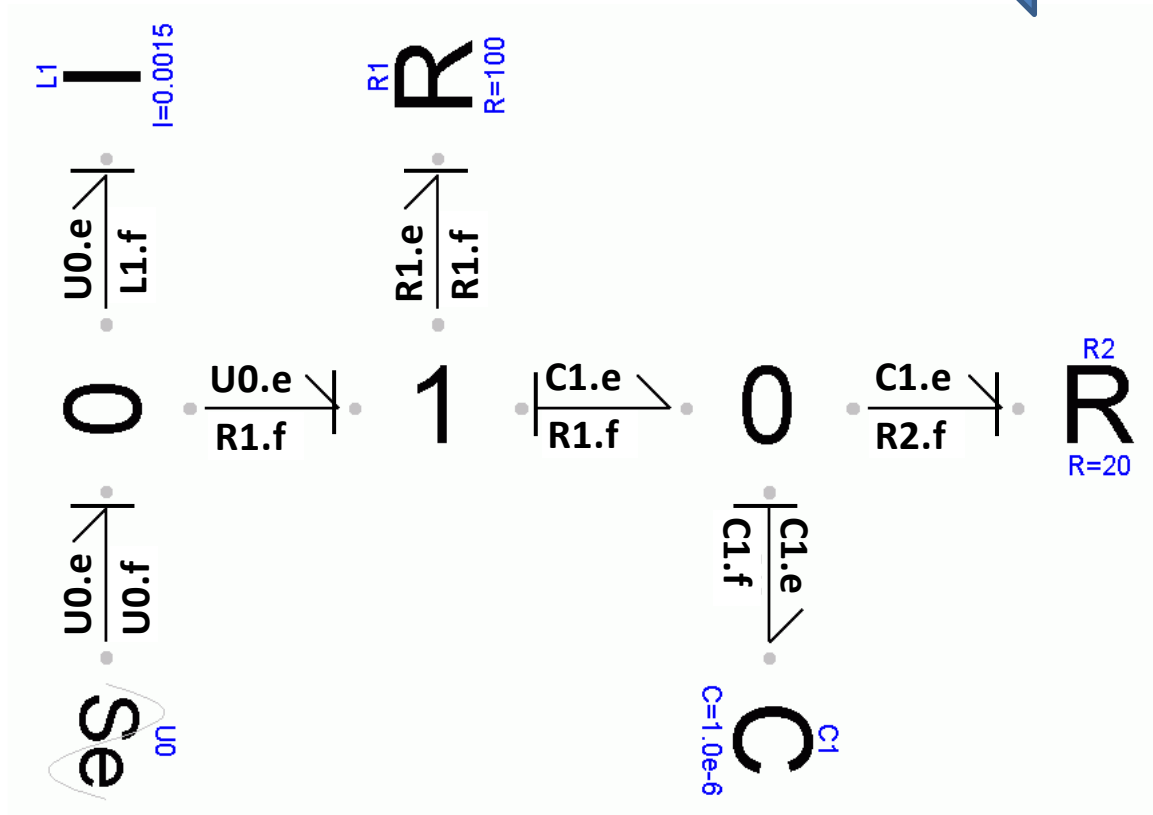


- An electrical energy domain model

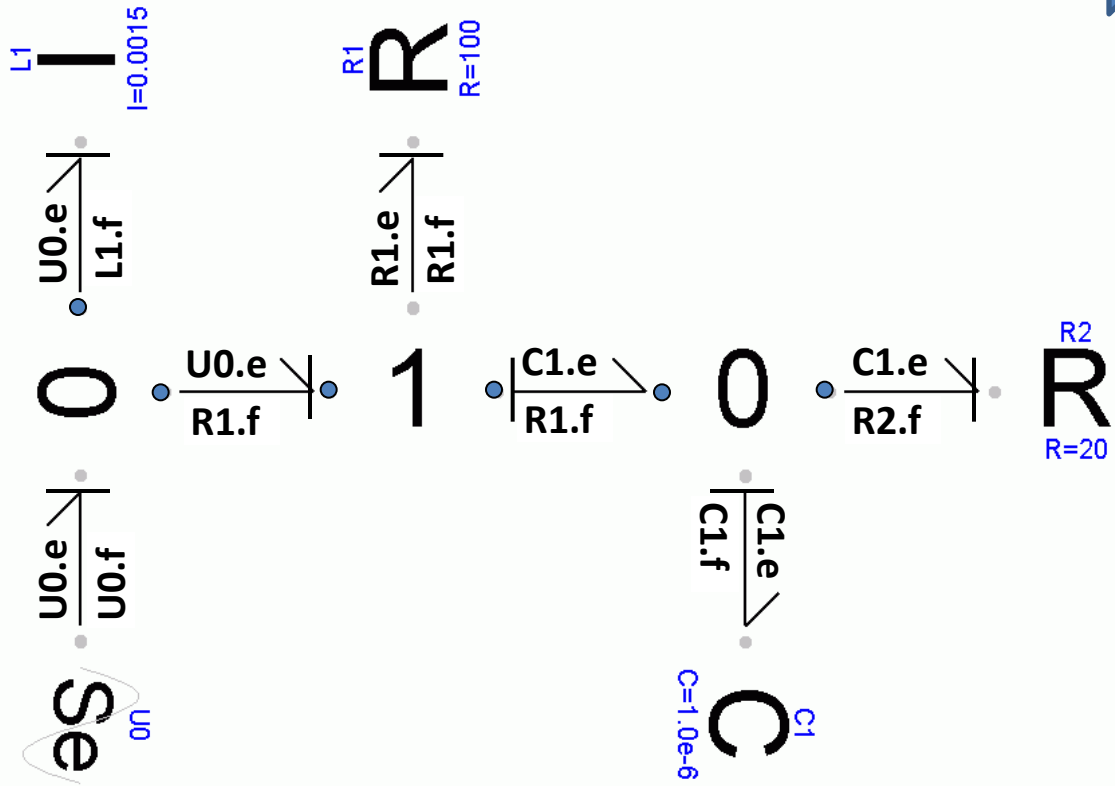
Bondgraphic equivalent



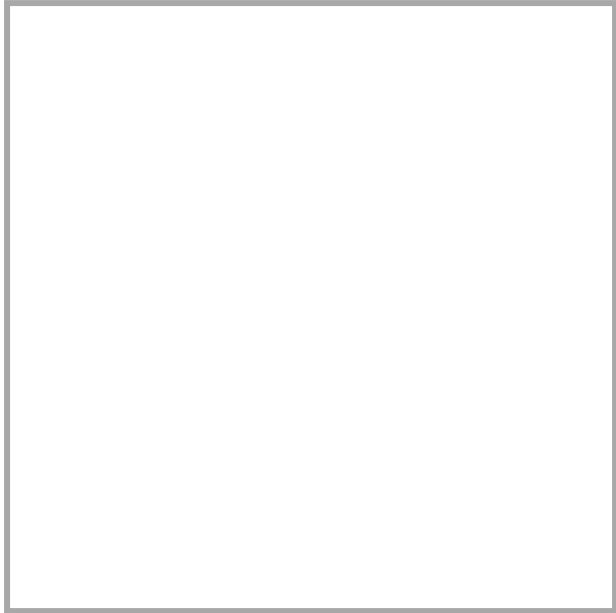
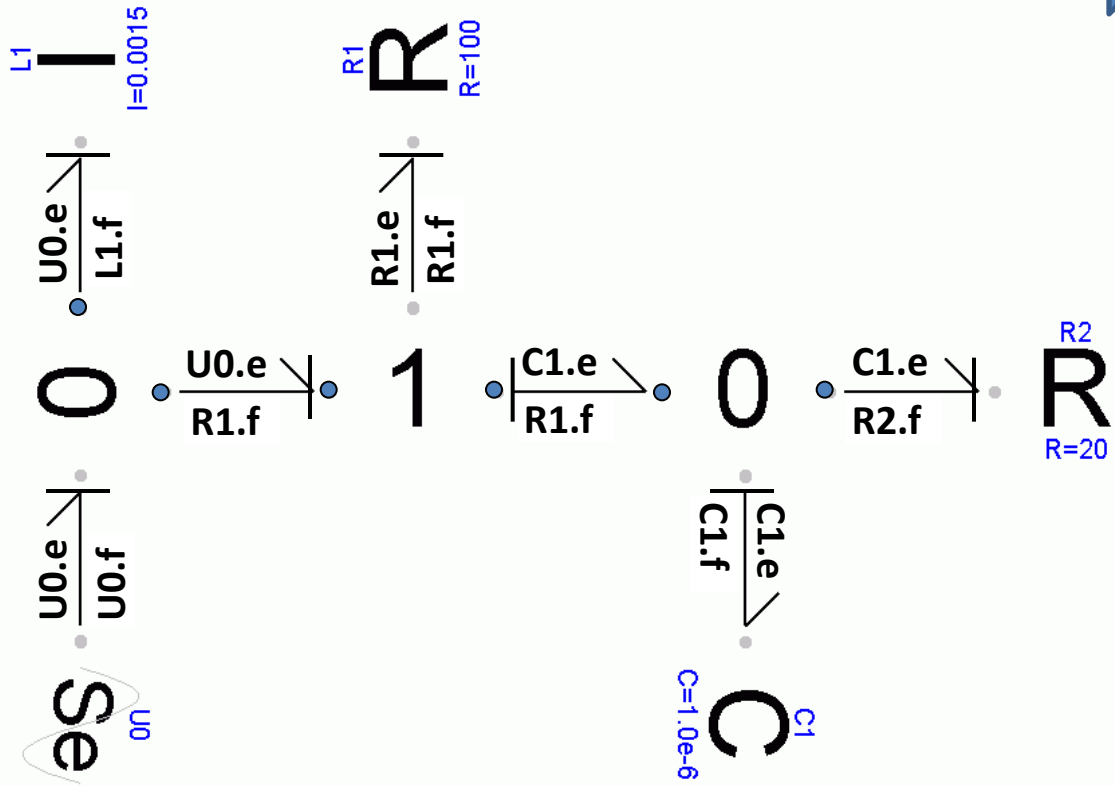
Electrical Circuit



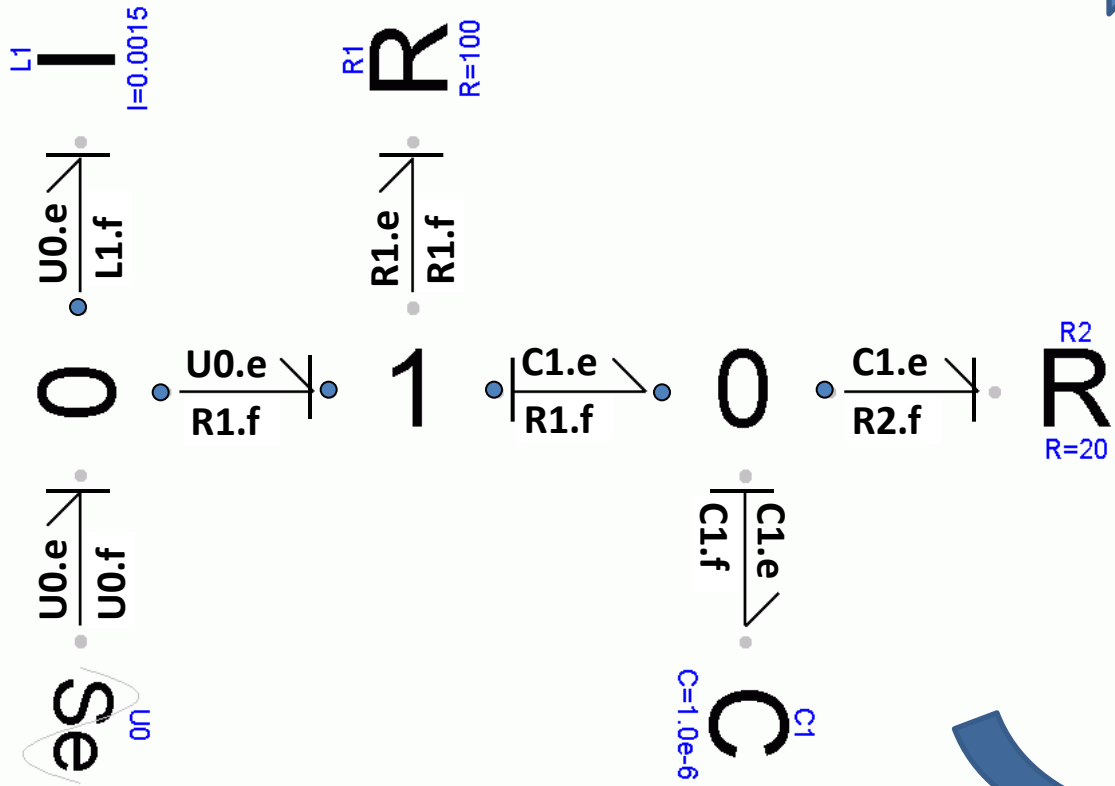
Bondgraphic model



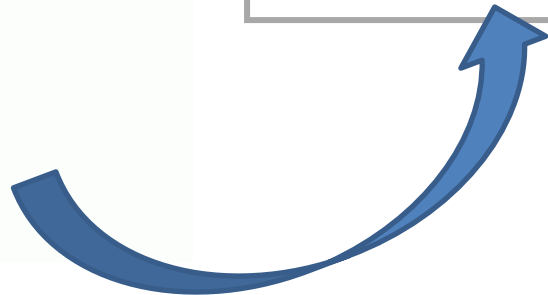
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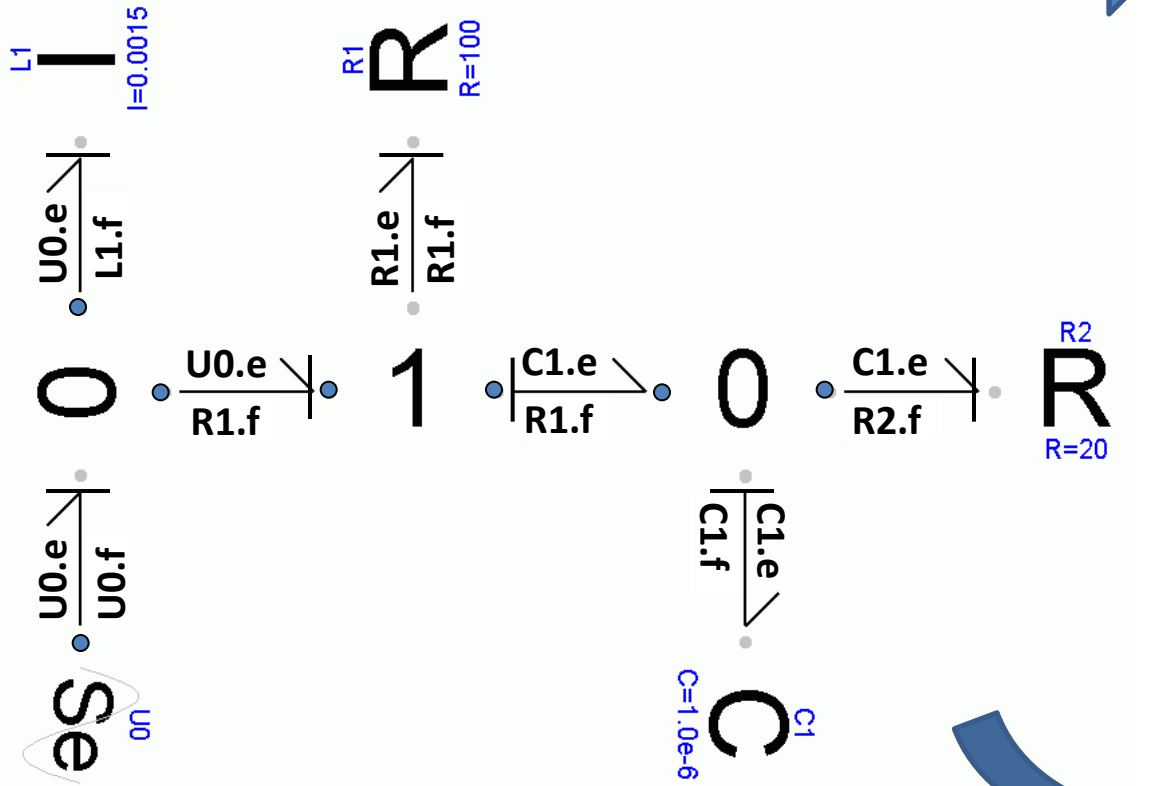
Bondgraphic model



Systematic derivation
of equations



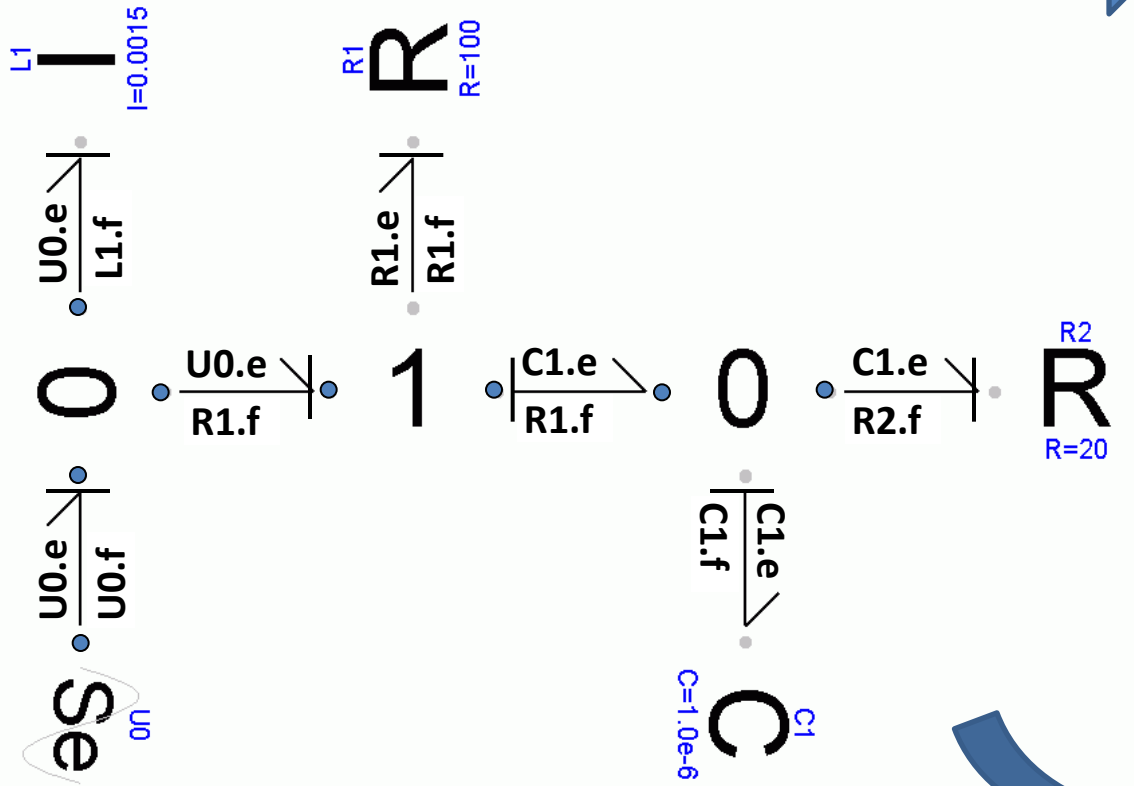
Bondgraphic model



Systematic derivation of equations

$$U0.e = f(t)$$

Bondgraphic model

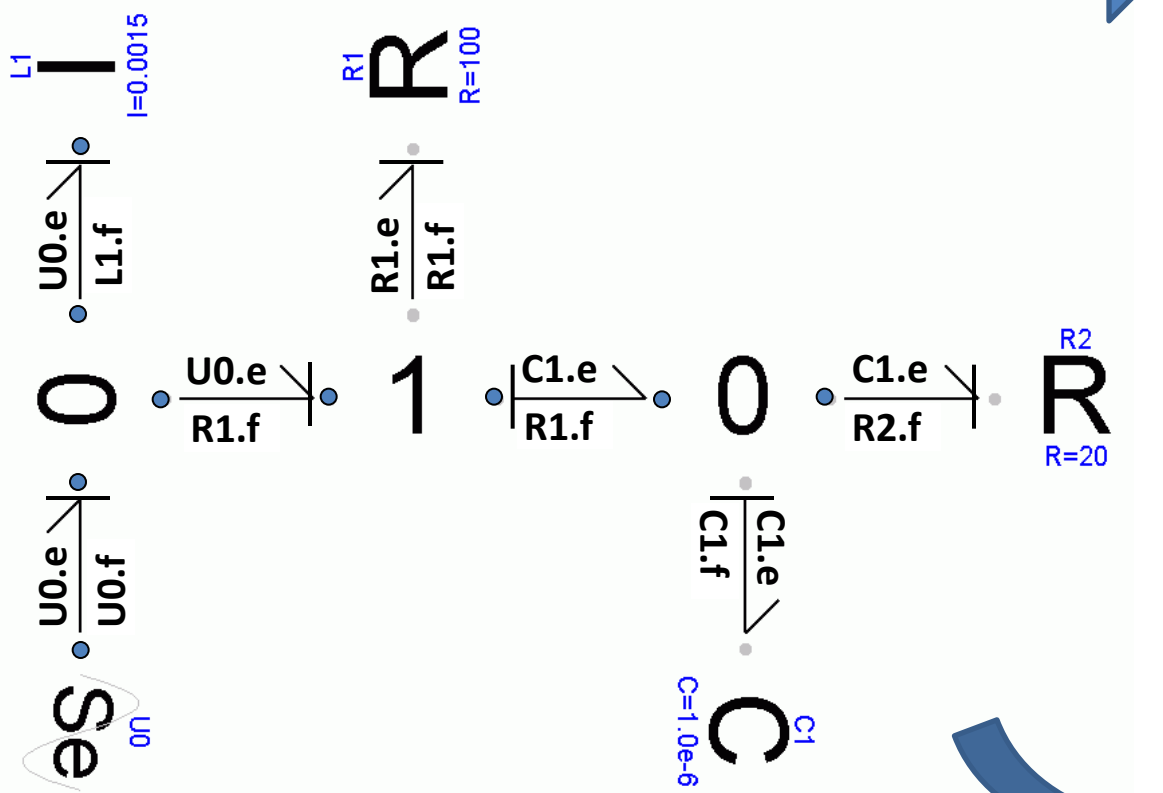


Systematic derivation of equations

$$U0.e = f(t)$$

$$U0.f = L1.f + R1.f$$

Bondgraphic model



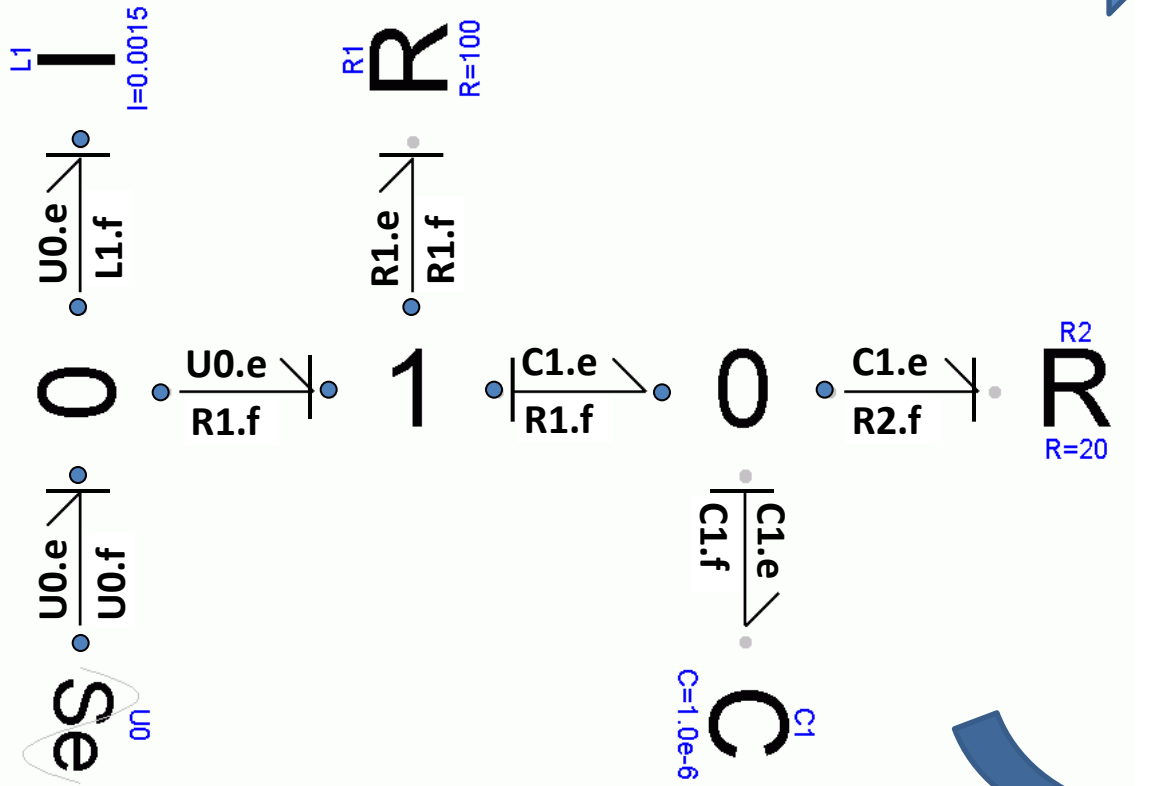
Systematic derivation of equations

$$U0.e = f(t)$$

$$U0.f = L1.f + R1.f$$

$$d/dt L1.f = U0.e / L1$$

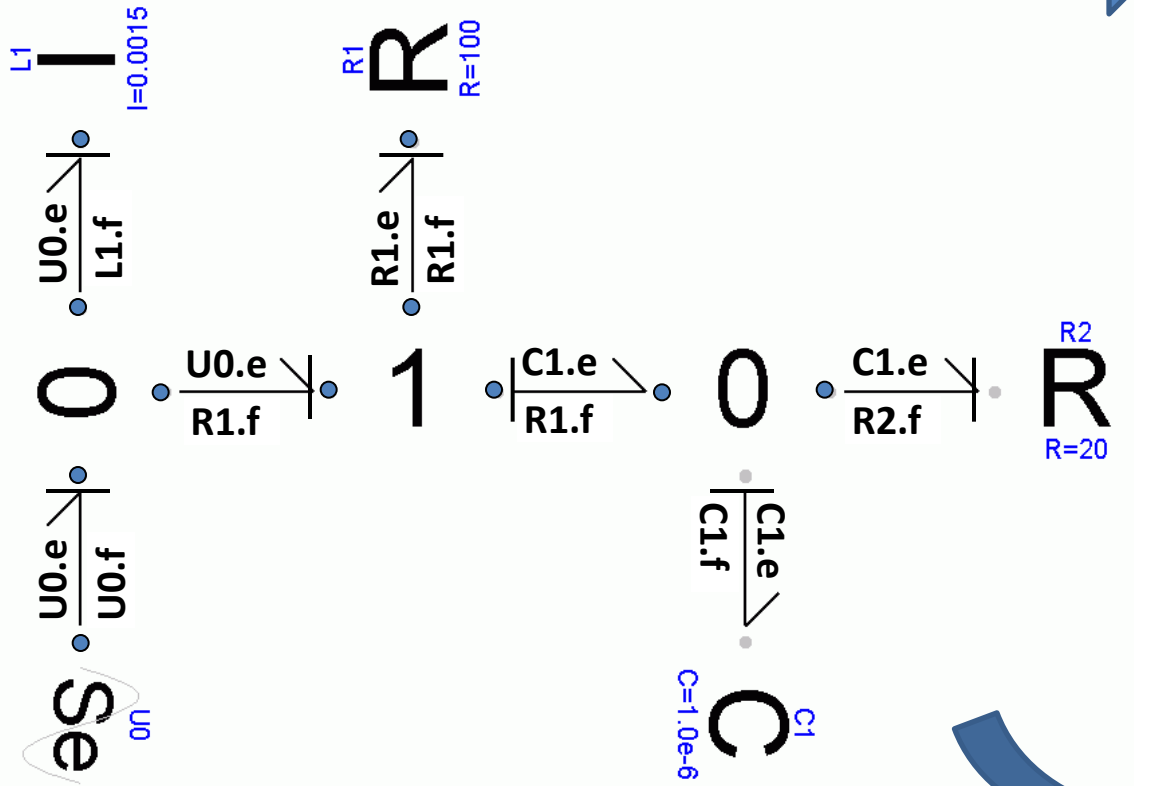
Bondgraphic model



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 R1.e &= U0.e - C1.e
 \end{aligned}$$

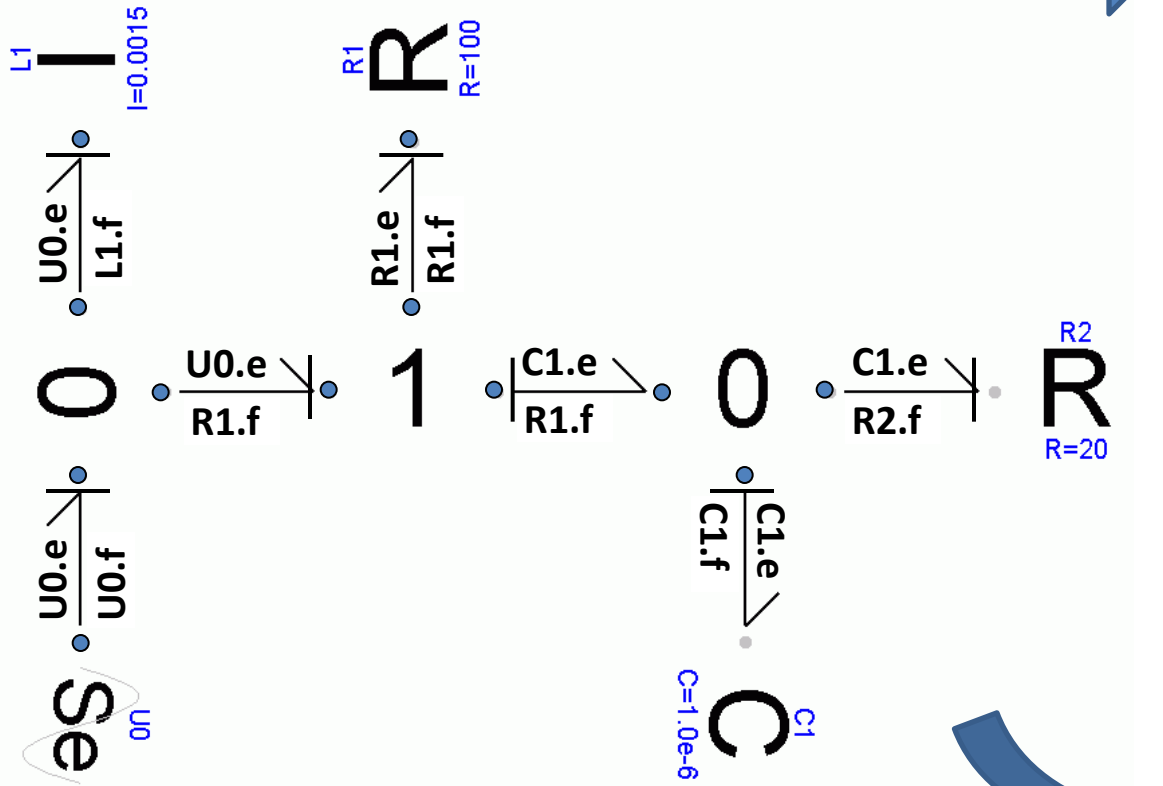
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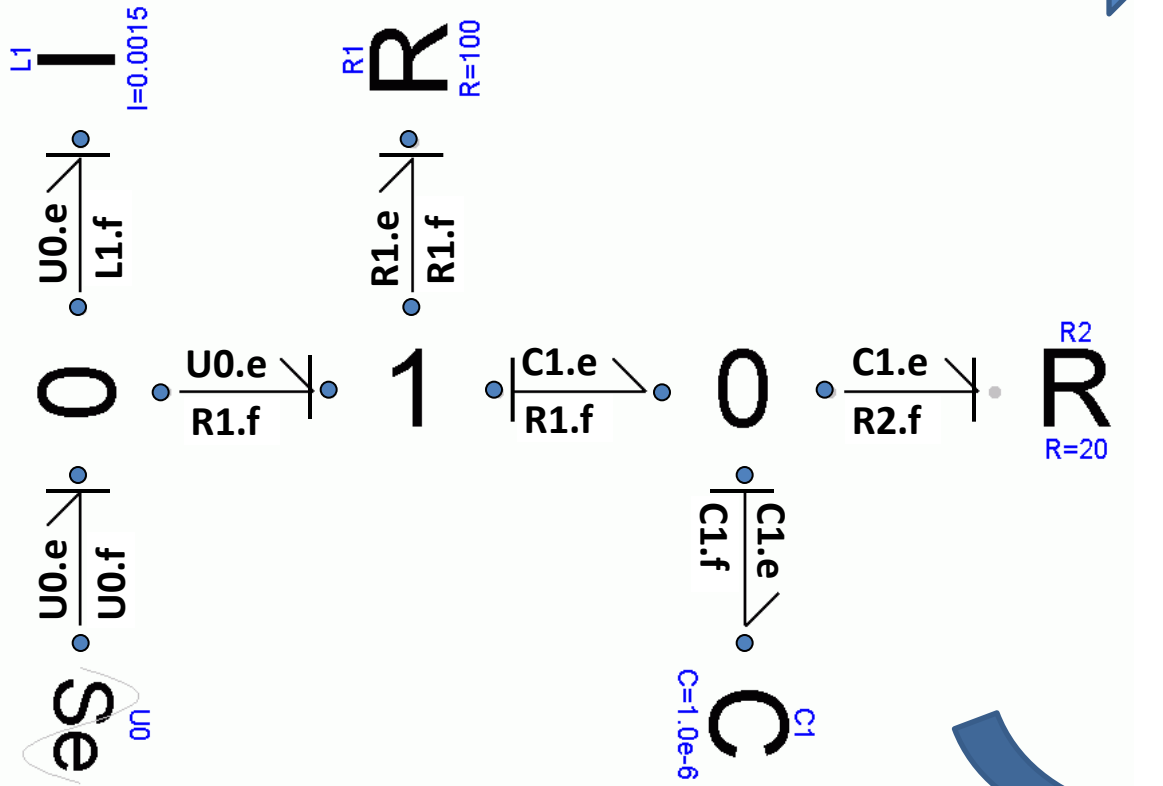
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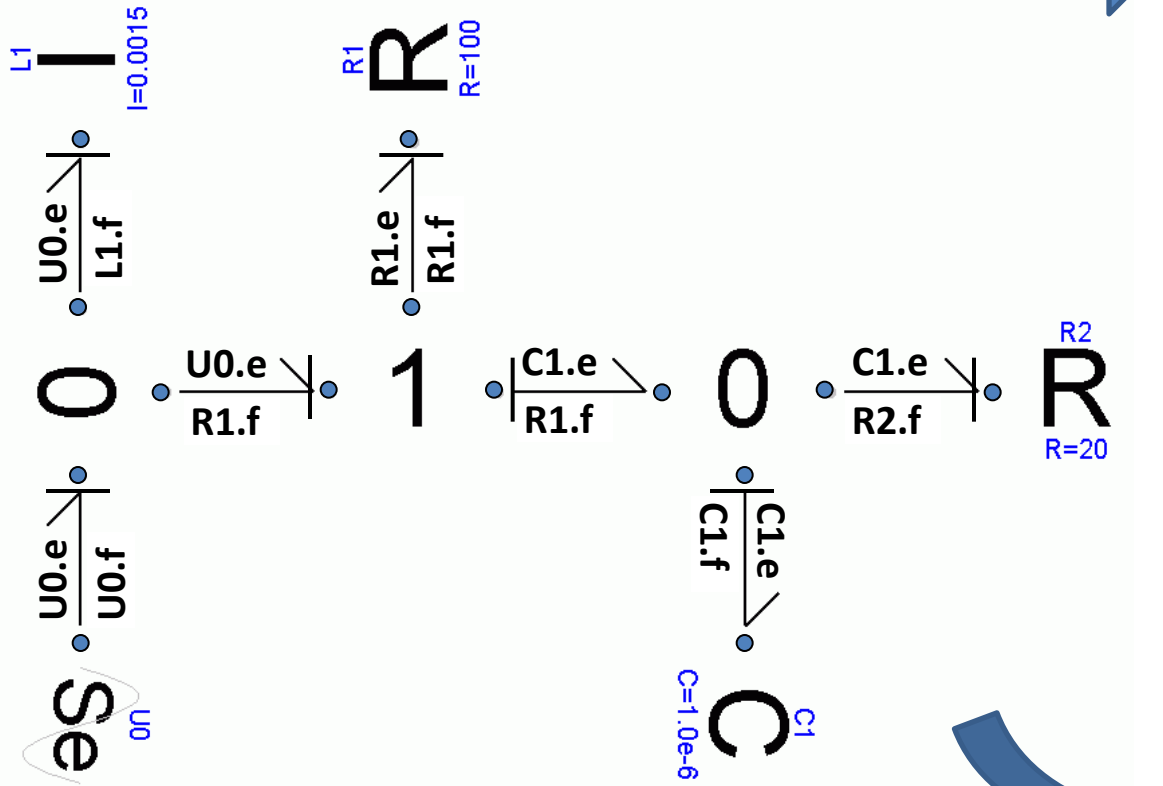
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 \end{aligned}$$

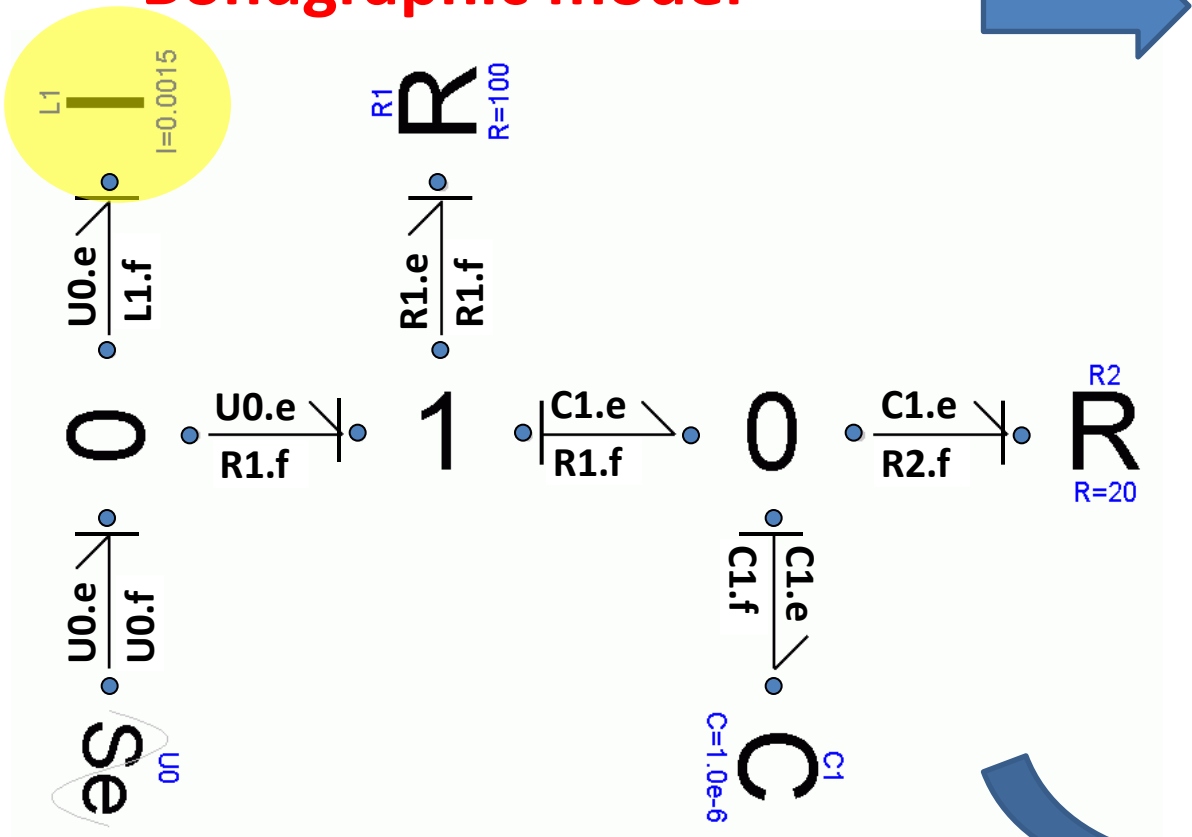
Bondgraphic model



Systematic derivation of equations

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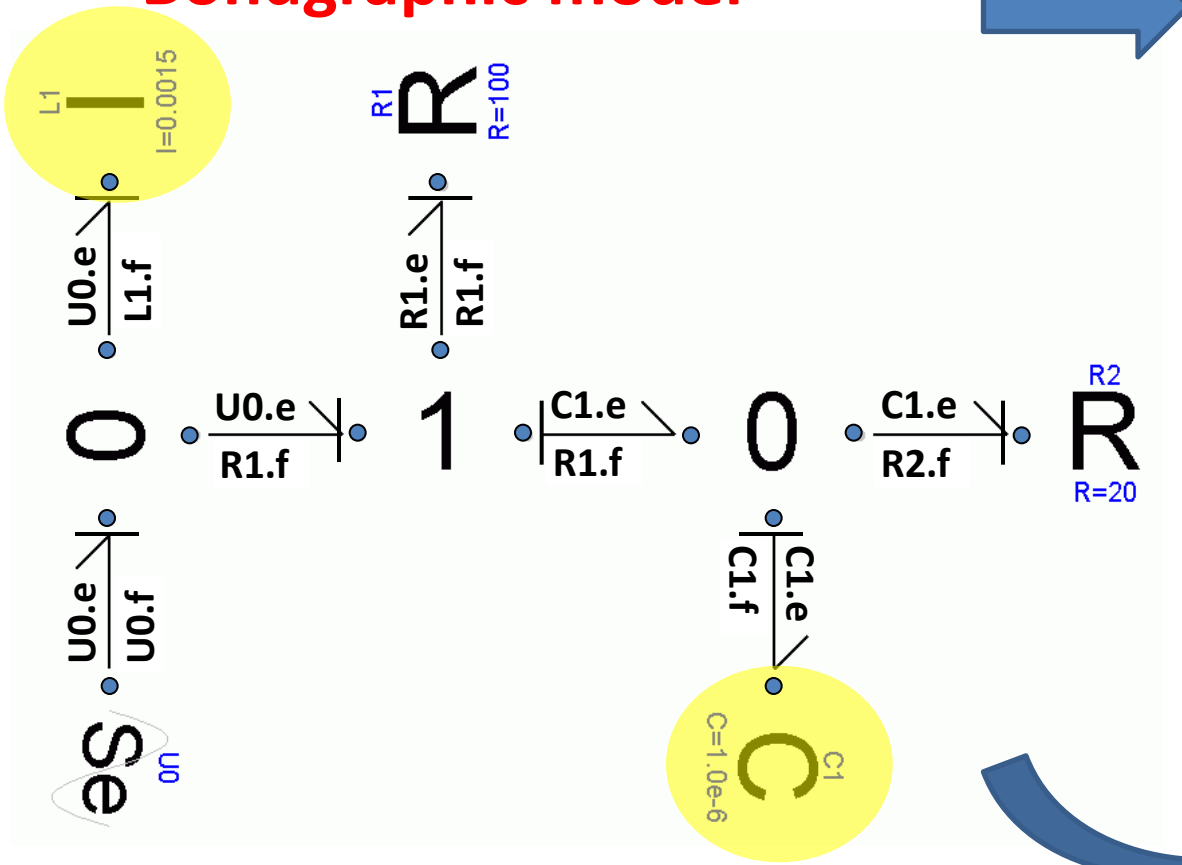
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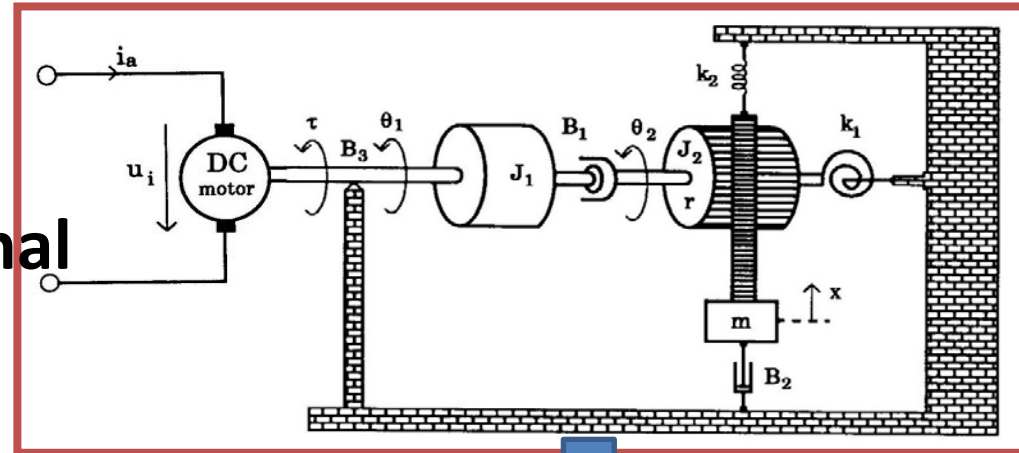
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Systematic derivation of equations

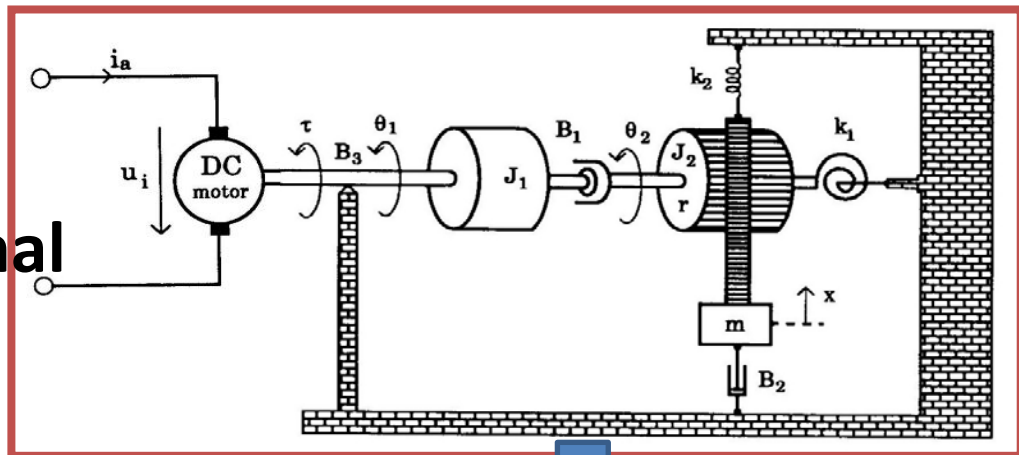
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- A multi-energy domain model
 - Electricity
 - Mechanical rotational
 - Mechanical translational

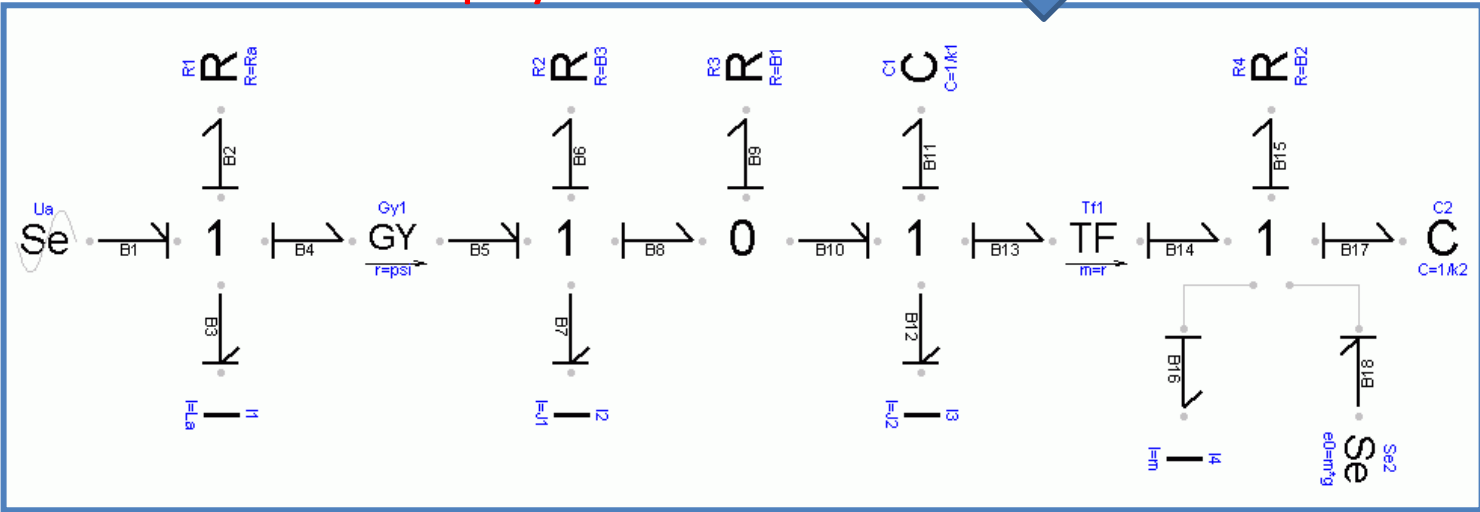


Special elements such as **Gyrator** and **Transformer** convert energy flows across diff. physical domains

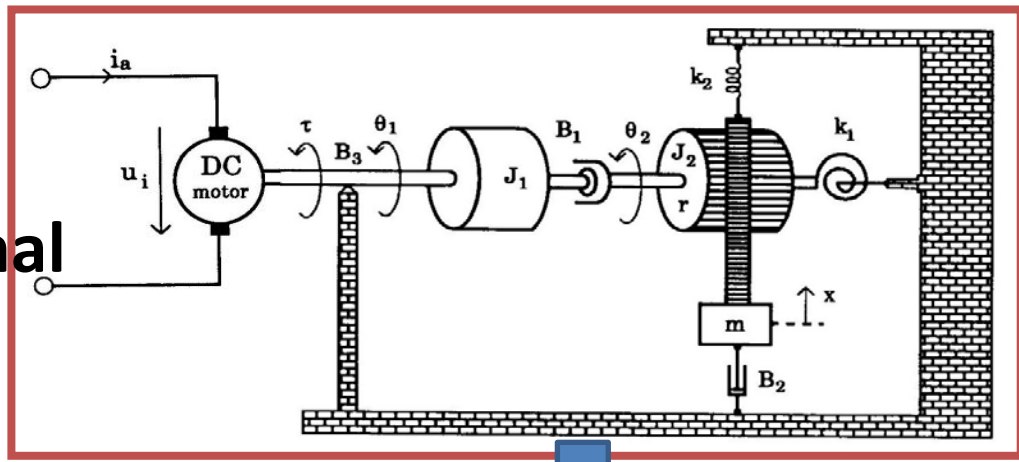
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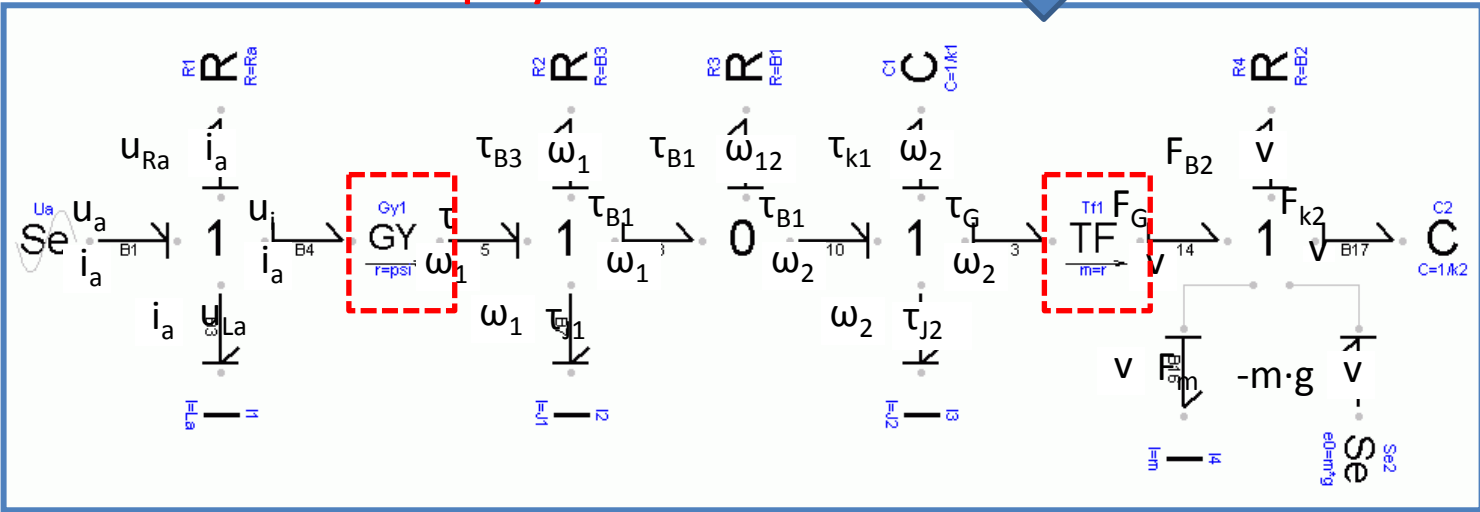
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Special elements such as **Gyrator** and **Transformer** convert energy flows across diff. physical domains



- Bond Graph variables for Complex Systems

- Facets 1 and 2

- Power variables:

- **Specific Enthalpy** [J/kg] (*an effort variable*)

- **Mass Flow** [kg/sec] (*a flow variable*).

[J/sec] = [J/kg] · [kg/sec] represents **power**

- Information variable

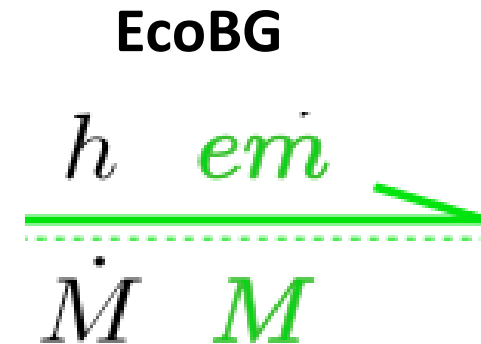
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- Facet 3 (the *emergy* facet)

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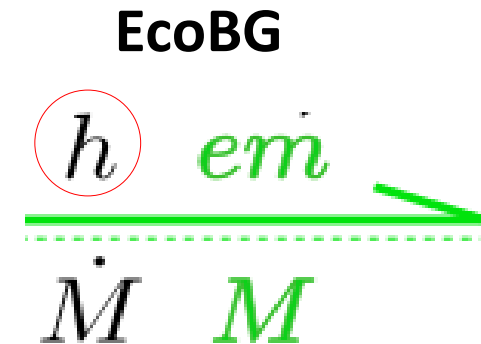
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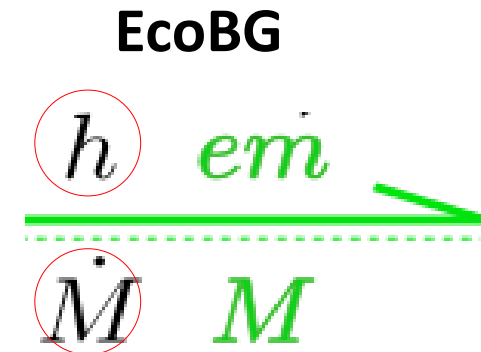
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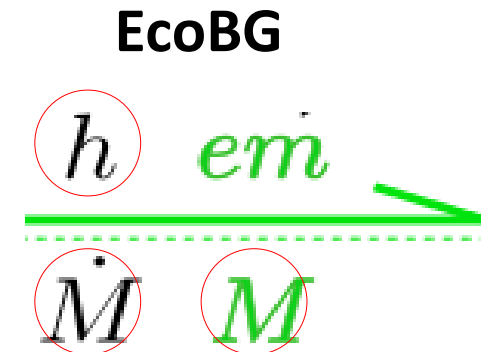
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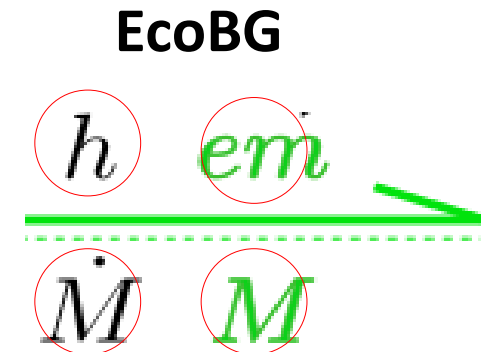
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- The EcoBG Storage element

- A **Capacitive Field (CF)** accumulates more than one quantity: Enthalpy, Mass and Emergy

$$\frac{e}{f} \rightarrow \text{C} \left\{ \begin{array}{l} q \\ c \end{array} \right. \quad e(t) = \frac{1}{C} \int f(t).dt \quad \left. \vphantom{\frac{e}{f}} \right\} \text{BG}$$

$$\frac{h \quad em}{\dot{M} \quad M} \rightarrow \text{CF} \left\{ \begin{array}{l} M \\ H \\ EM \\ h \end{array} \right. \quad \left. \vphantom{\frac{h \quad em}{\dot{M} \quad M}}} \right\} \text{EcoBG}$$

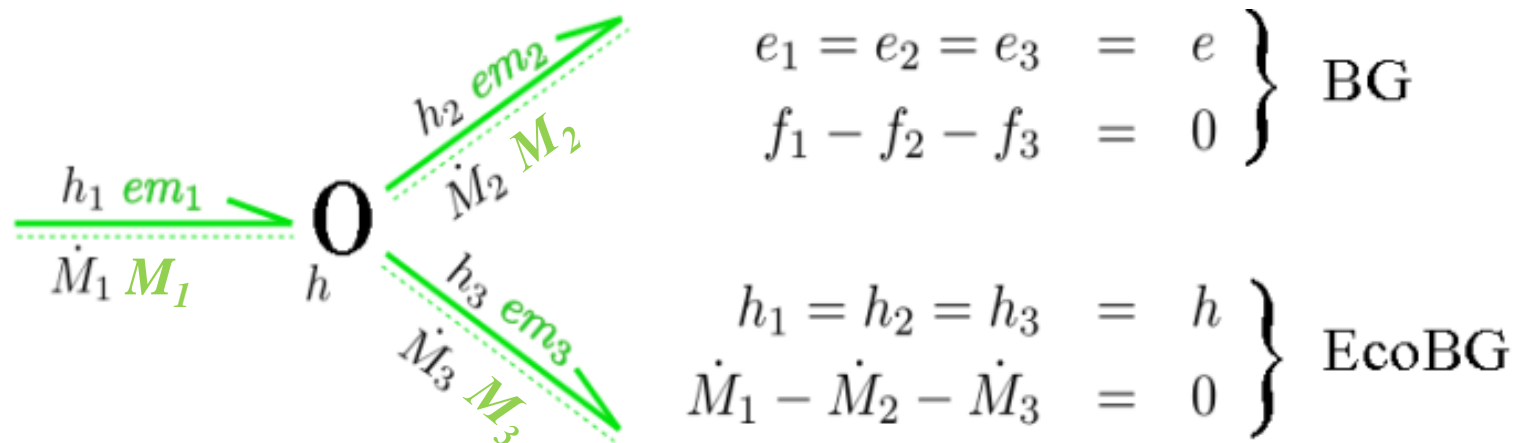
$$H(t) = h \int \dot{M}(t).dt$$

$$M(t) = H(t)/h$$

$$EM(t) = \int em(t).\dot{M}(t).dt$$

The **specific enthalpy** is
a property of the accumulated mass
 Known in advance -> A parameter

- The EcoBG 0-Junction

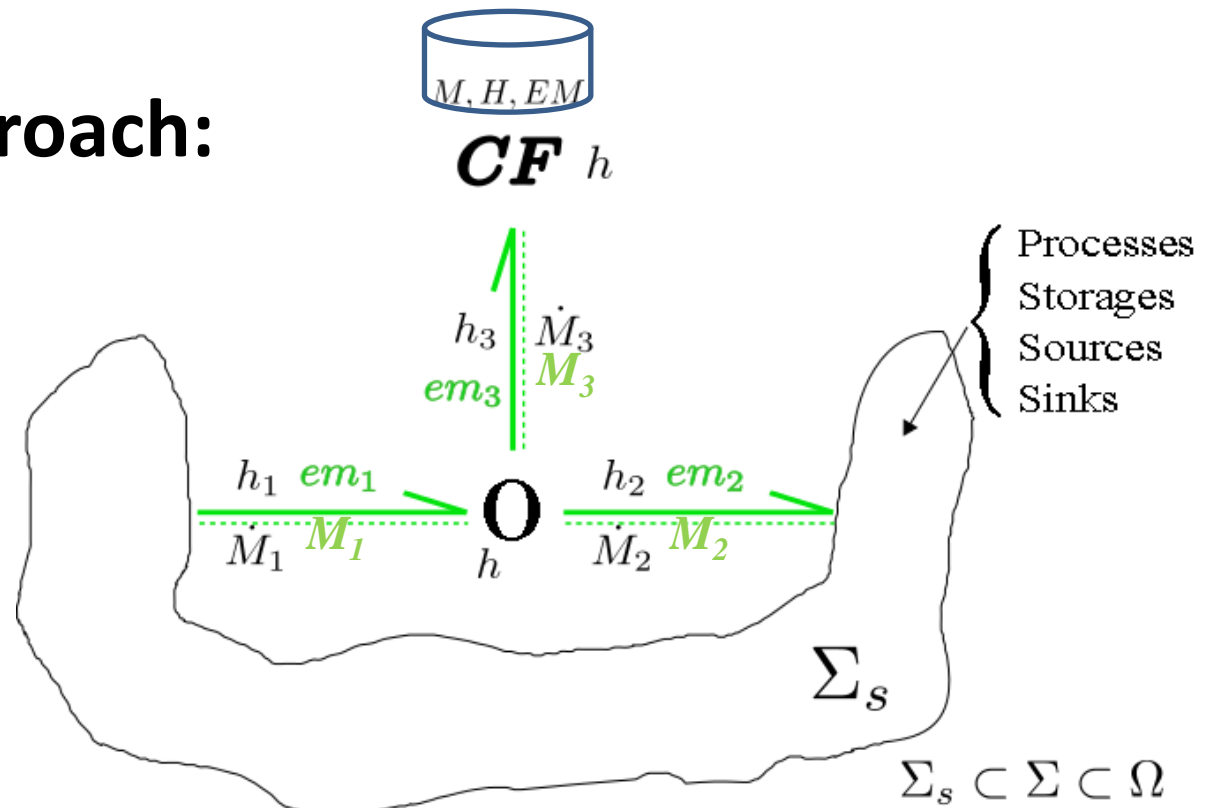


$$em_{in} = em_1 \quad em_{out} = em_2 = em_3$$

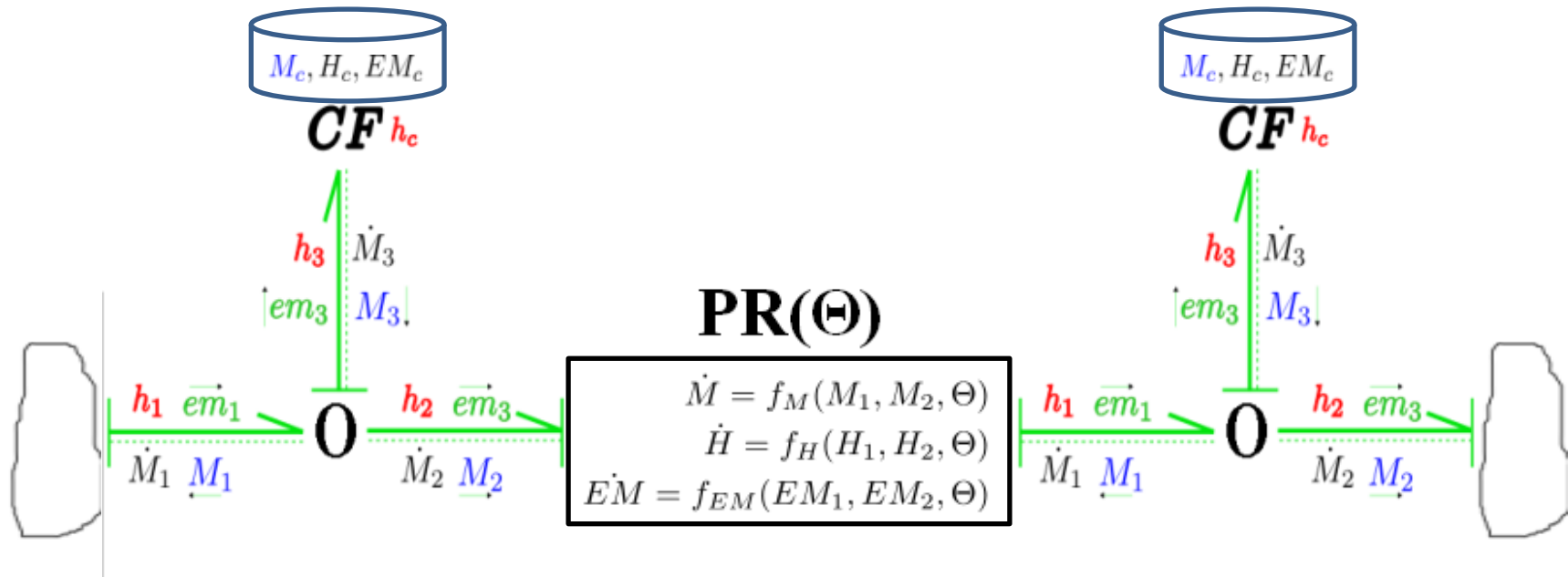
$$\left. \begin{aligned} \sum Power &= \sum \dot{H}_i = h \cdot \sum \dot{M}_i = 0 \\ \sum EmPower &= \sum E\dot{M}_i = \sum em_i \cdot \dot{M}_i = 0 \end{aligned} \right\} \text{Power Balances}$$

- Basic unit based on EcoBG elements
 - An important “building block”
- Storage of mass and energy adhering to the proposed

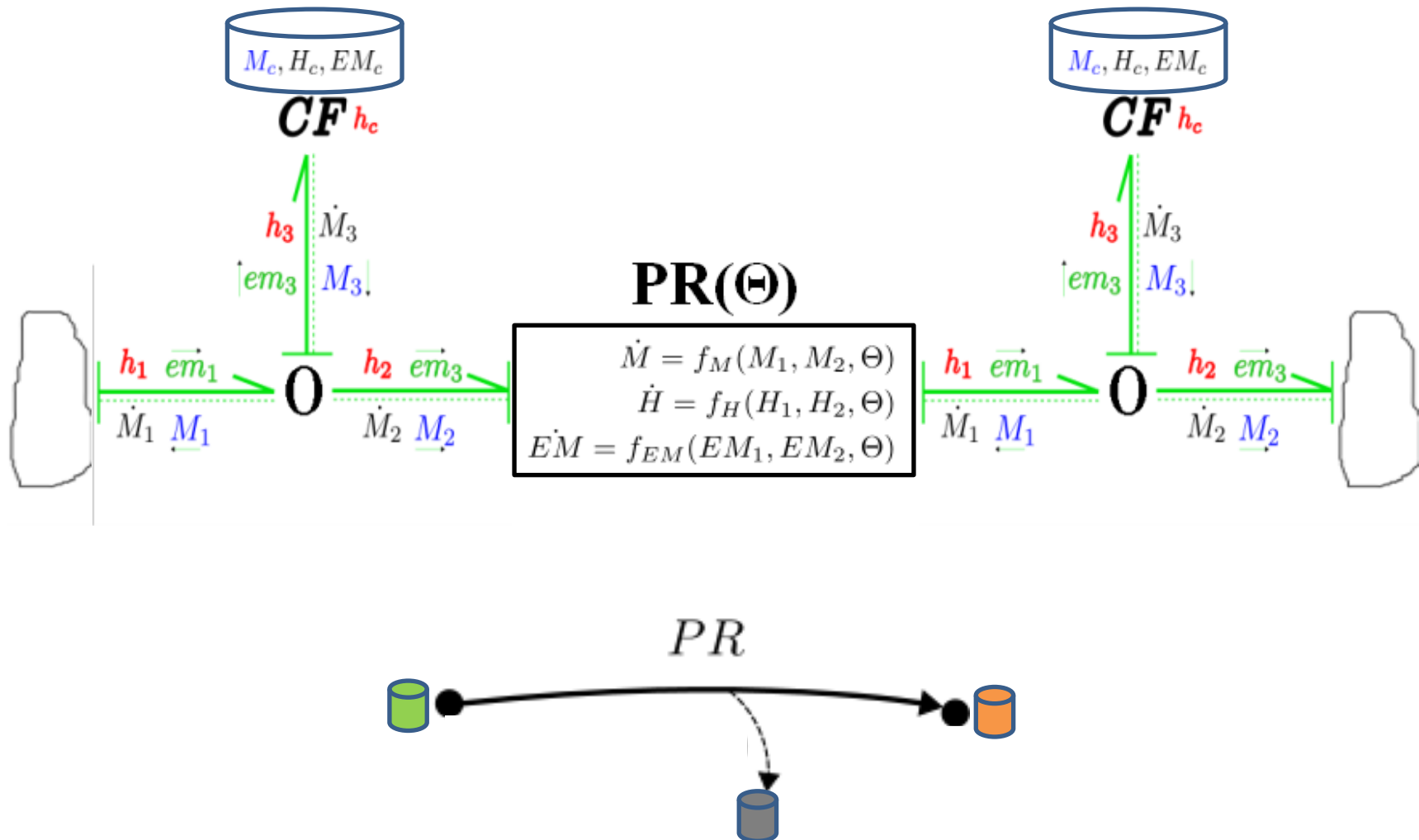
3-Faceted approach:



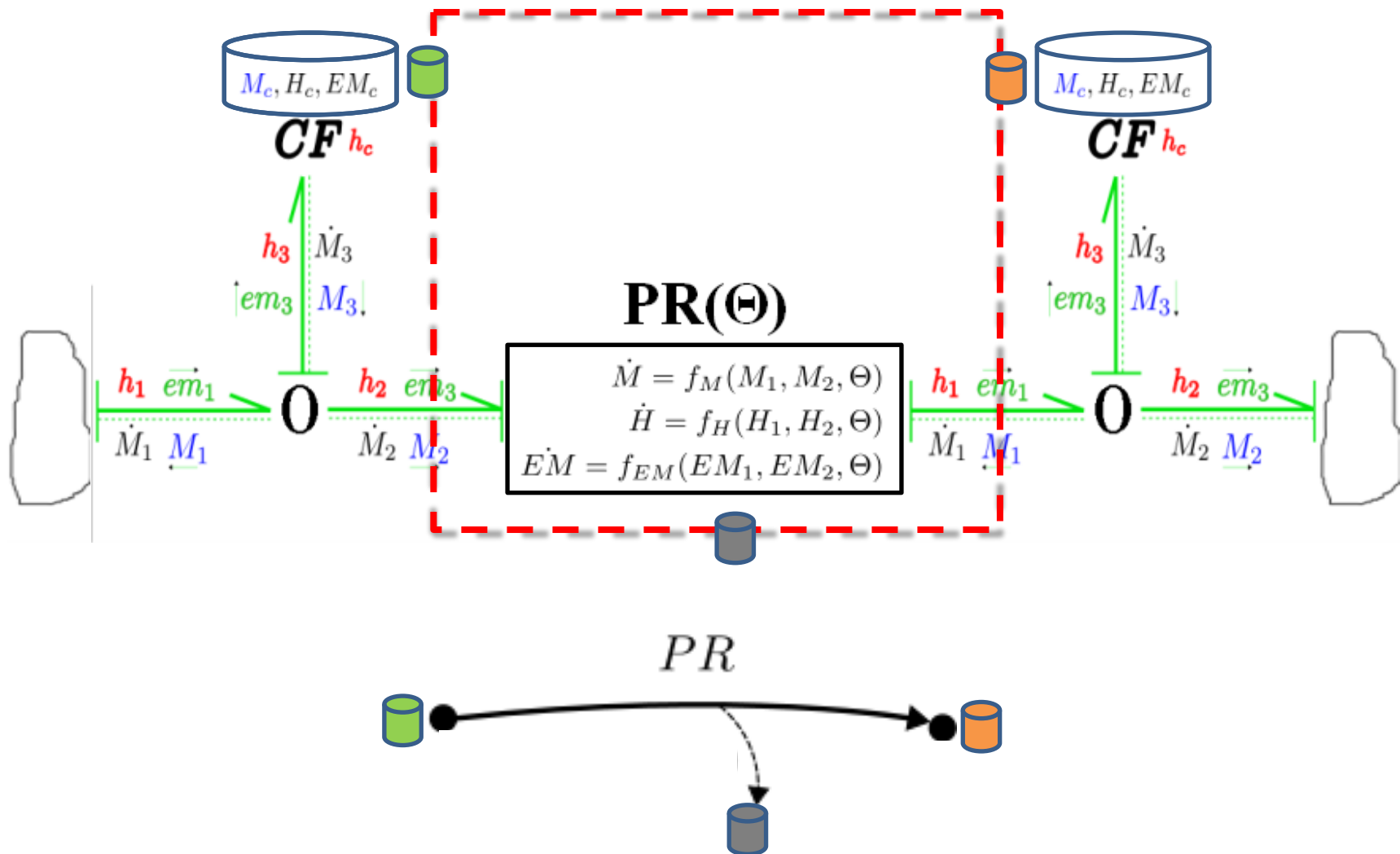
- EcoBG Process elements



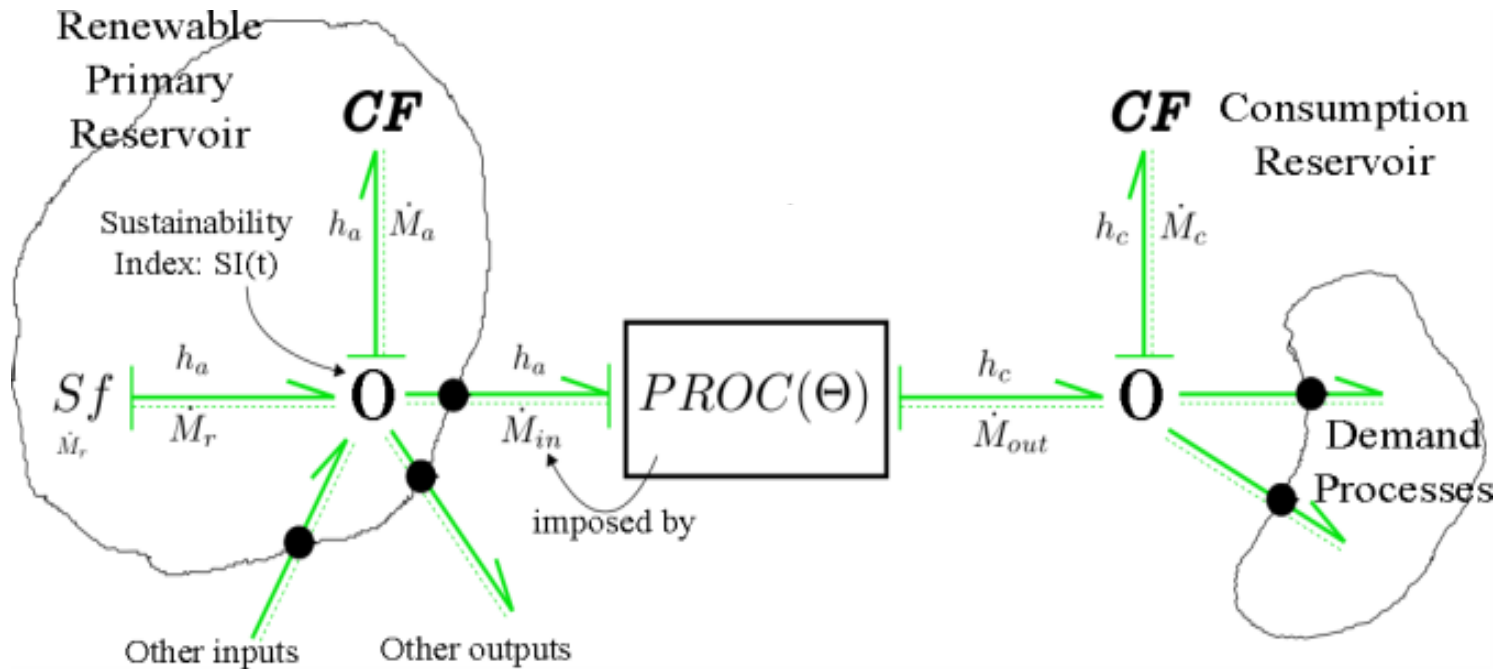
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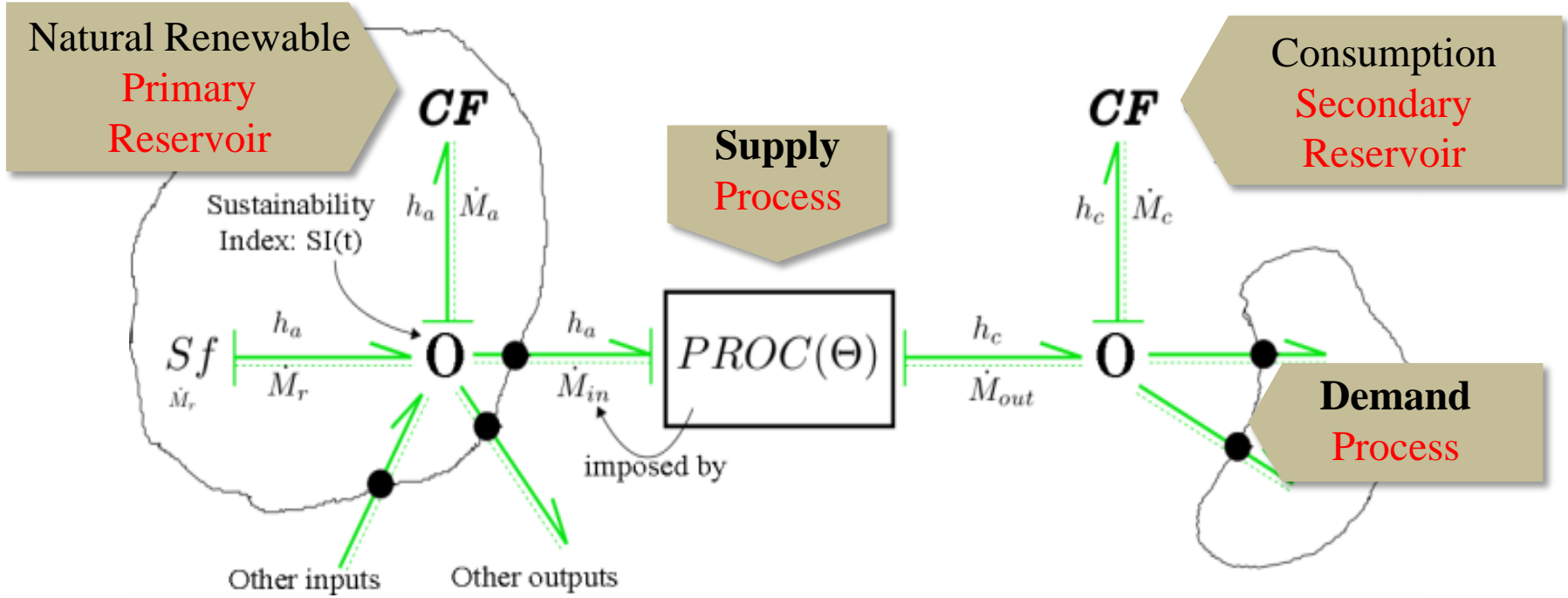
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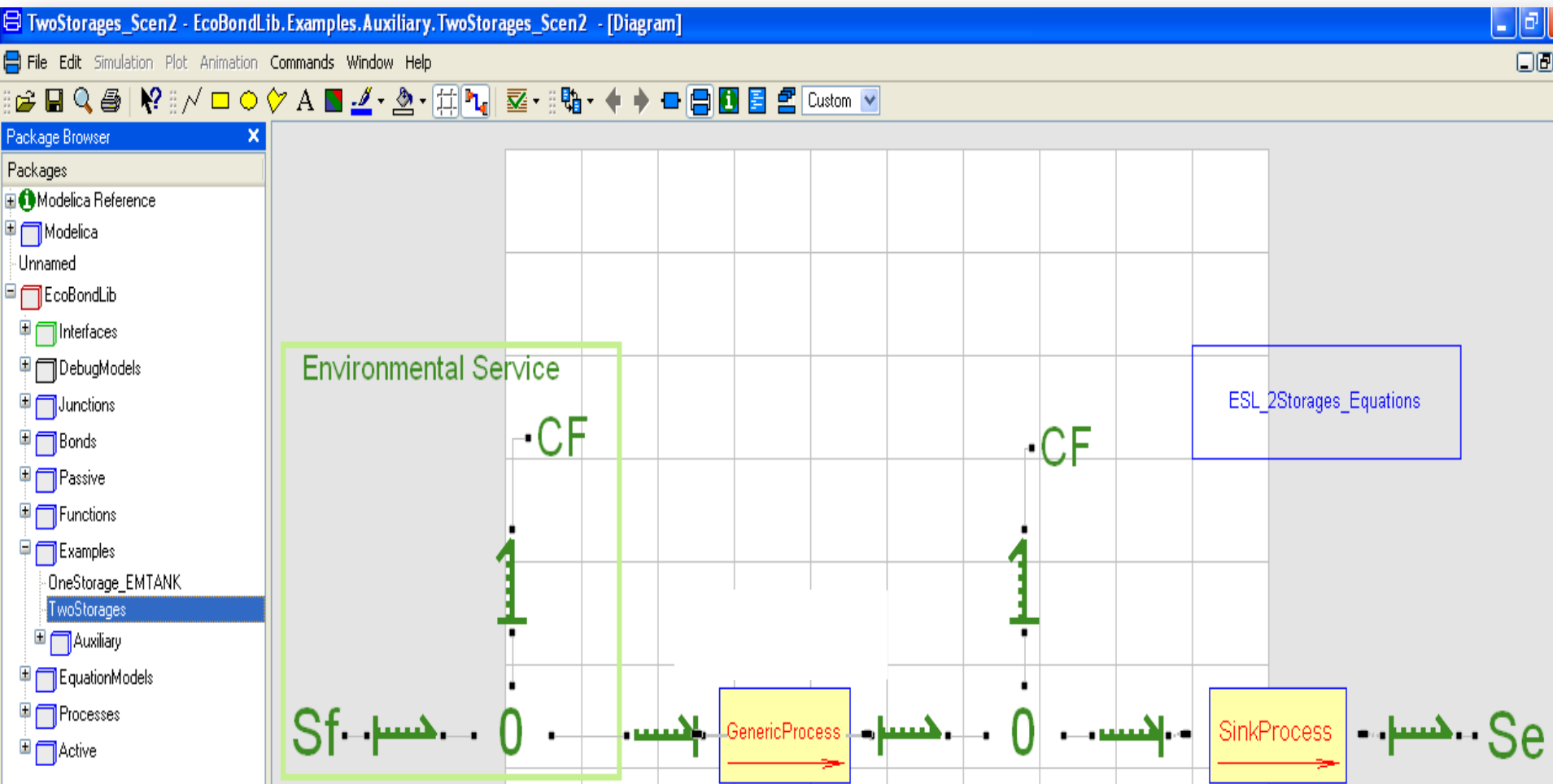
- Extraction of renewable resources for consumption



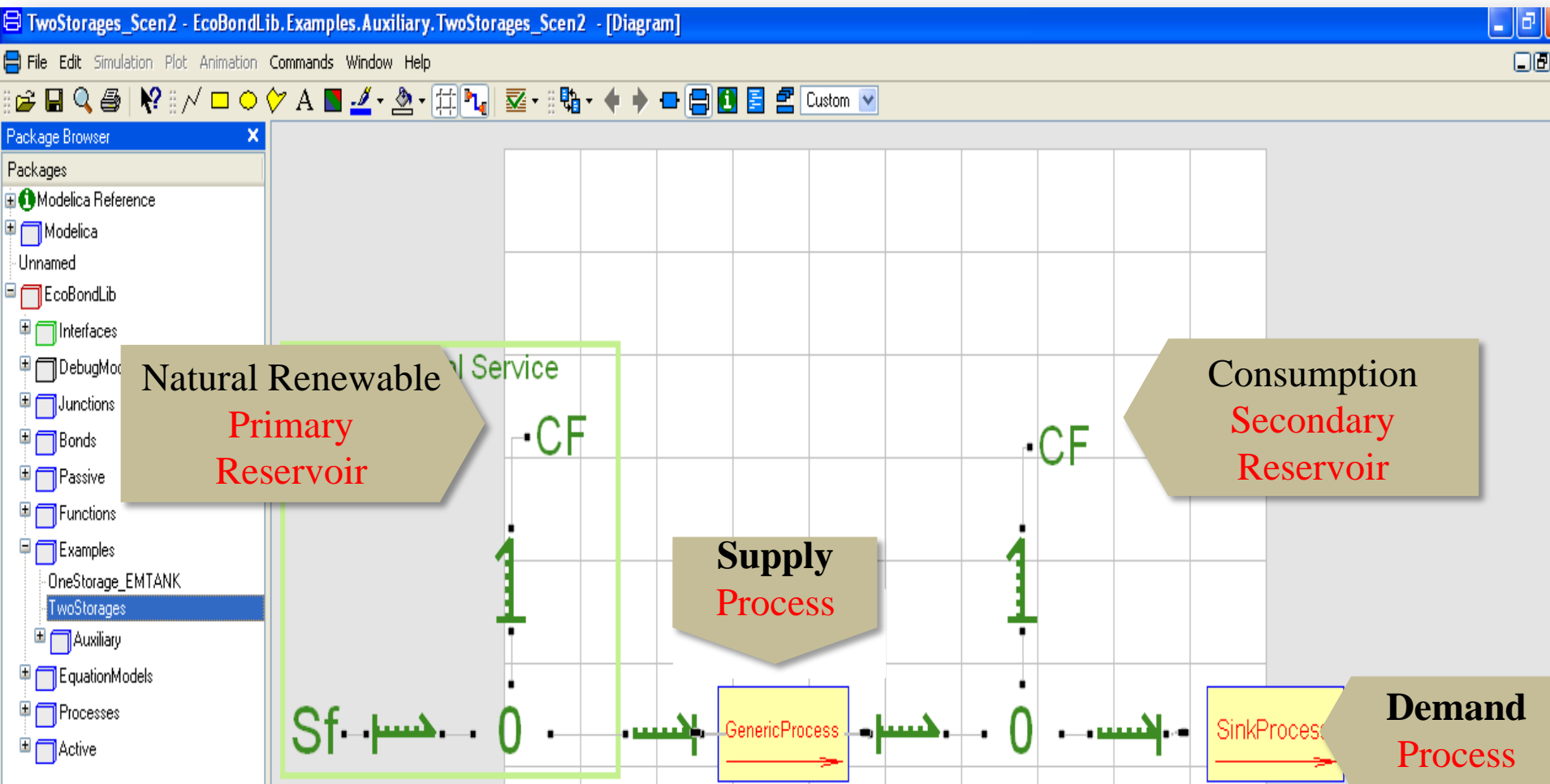
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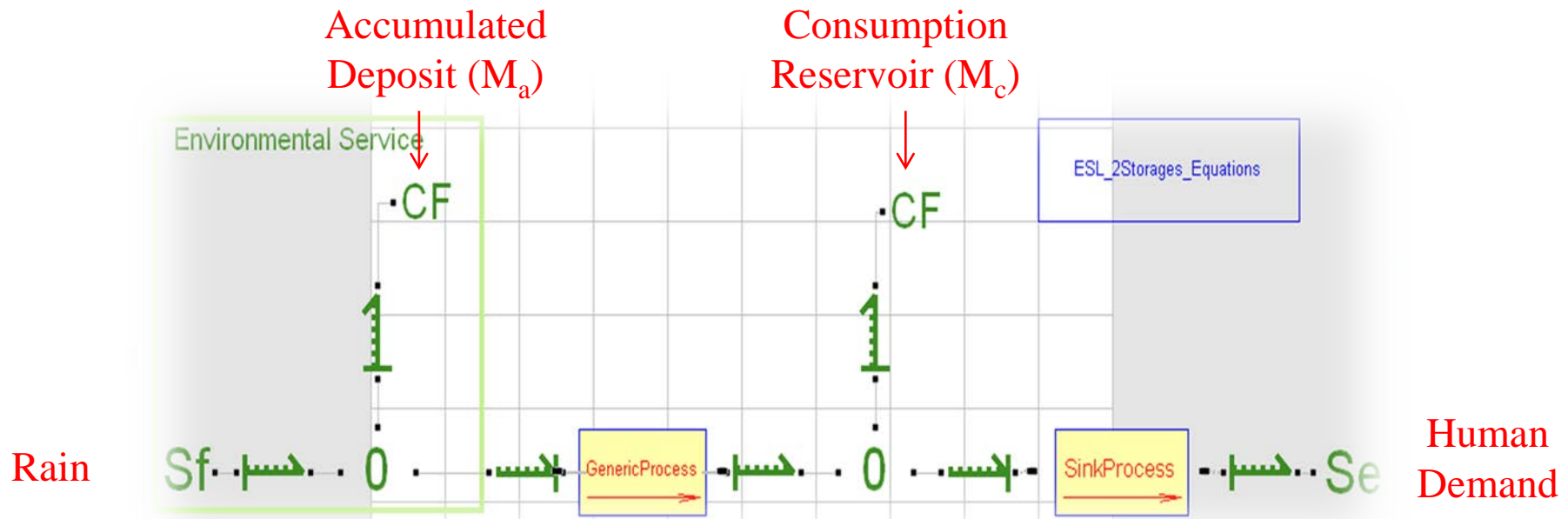


- EcoBG library implemented in the Dymola[®] tool.

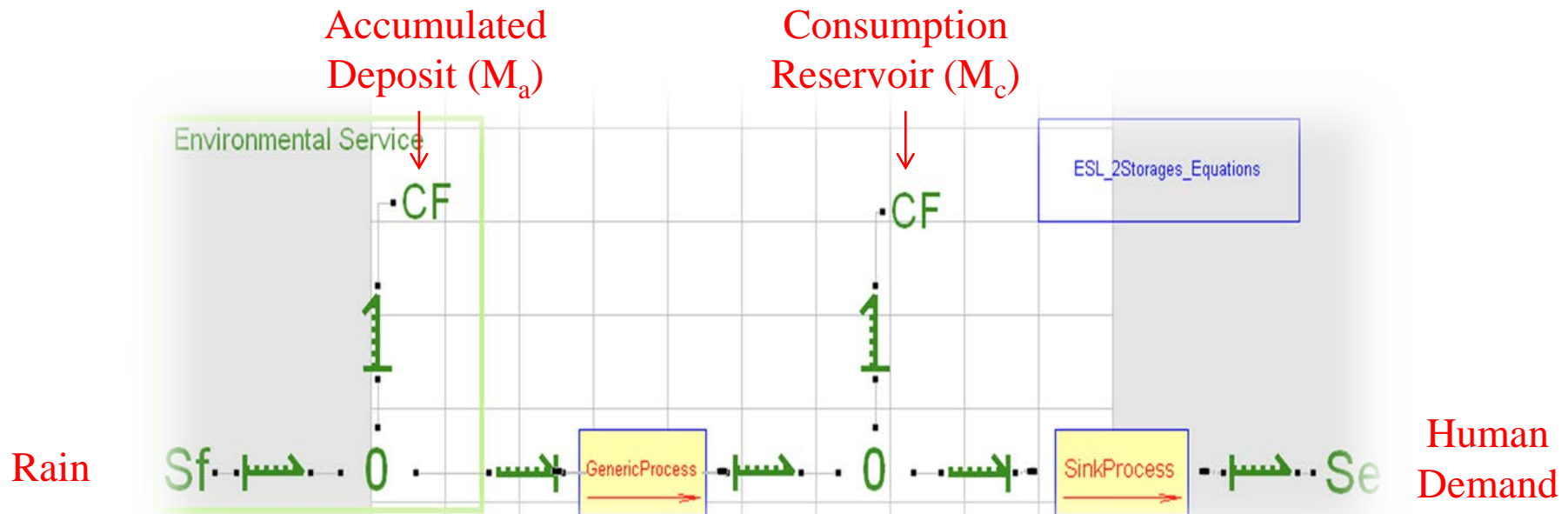


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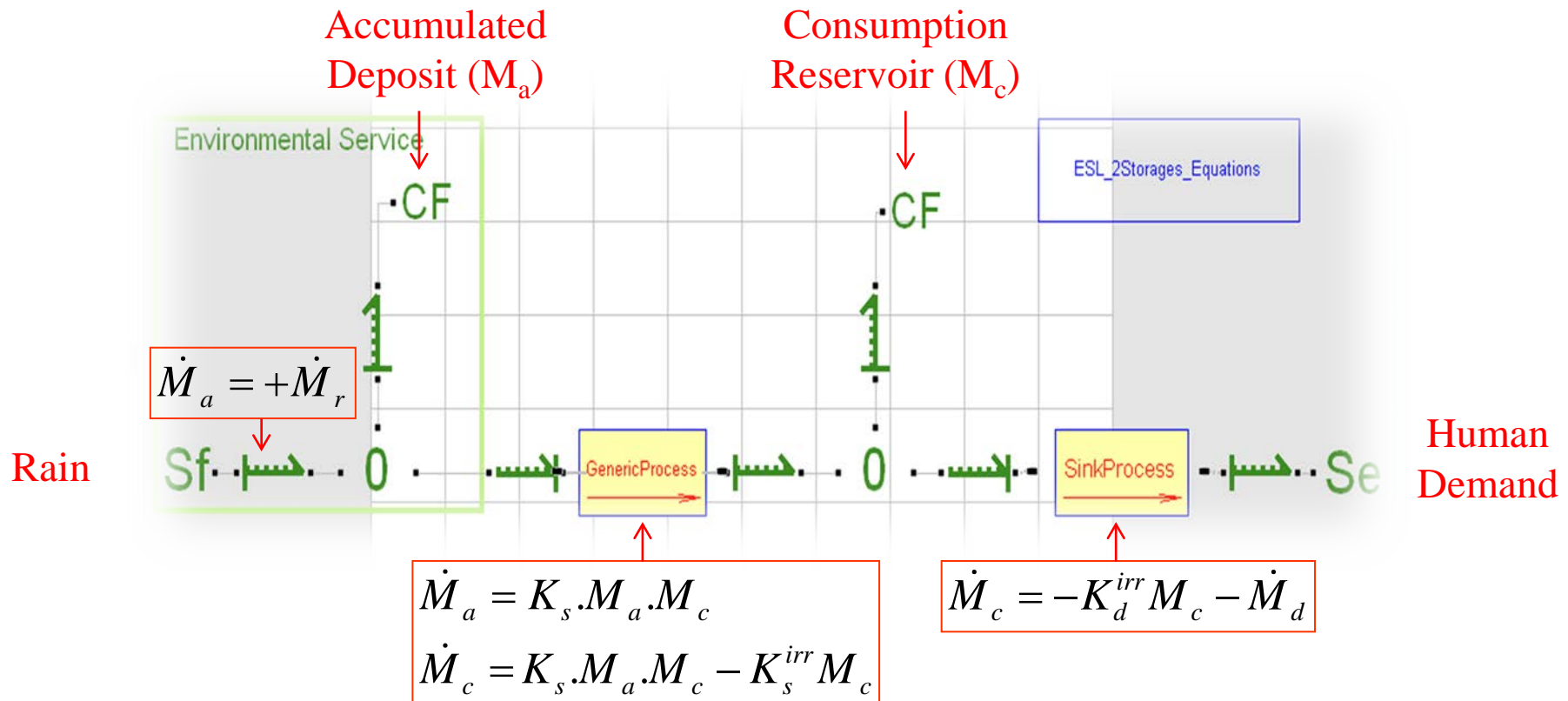




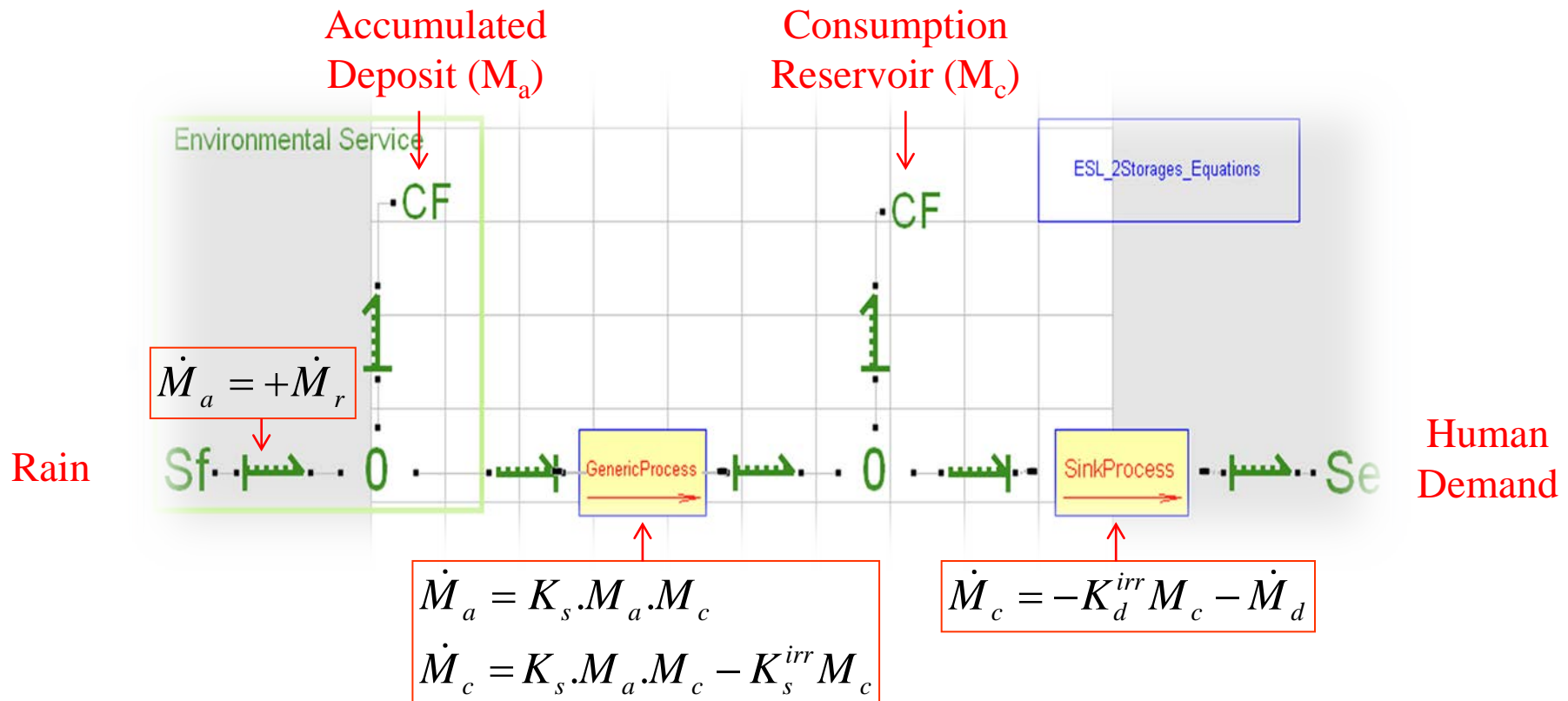
$$\begin{aligned} \dot{M}_a &= \dot{M}_r - K_s \cdot M_a \cdot M_c \\ \dot{M}_c &= K_s \cdot M_a \cdot M_c - K_s^{irr} M_c - \dot{M}_d \end{aligned}$$



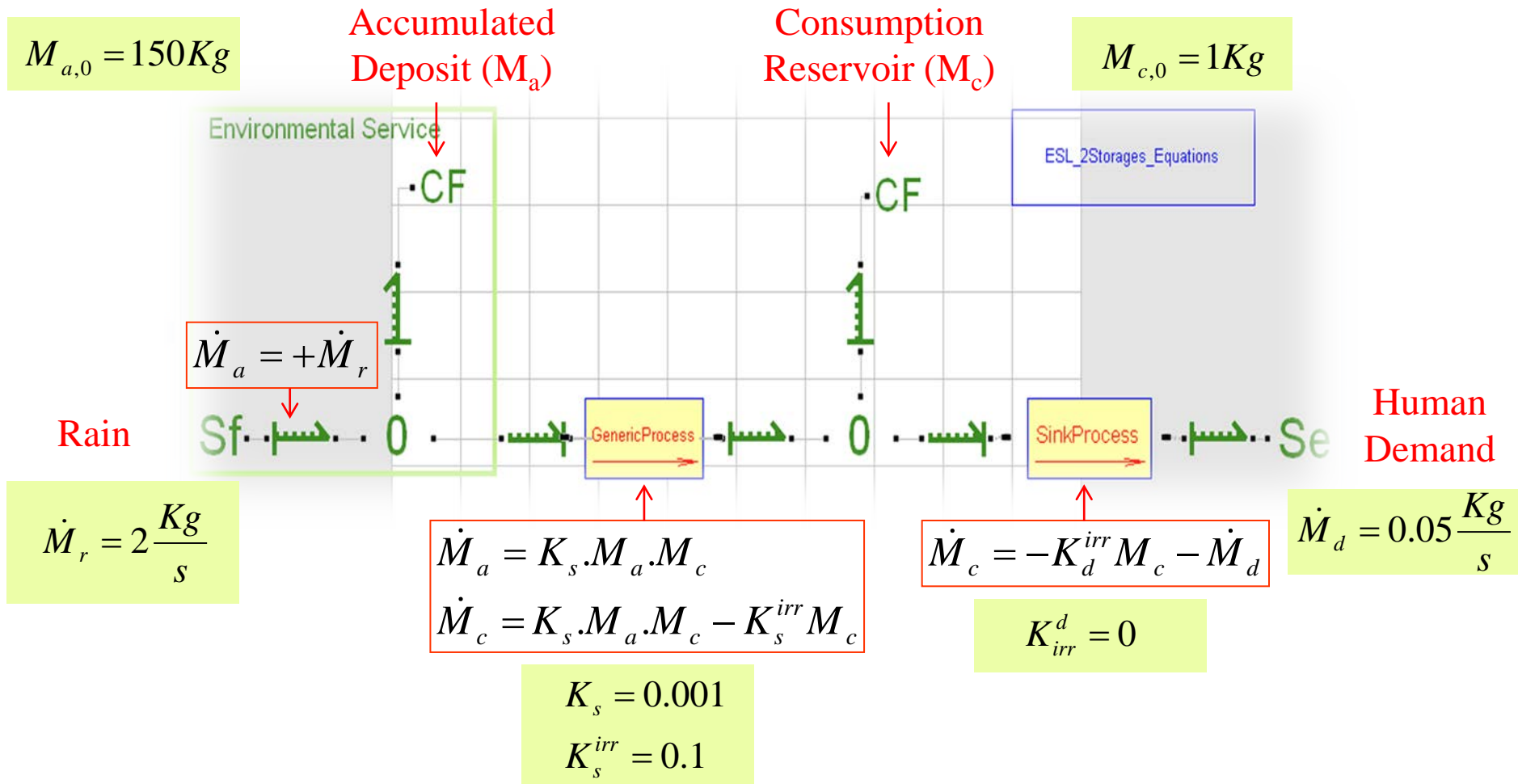
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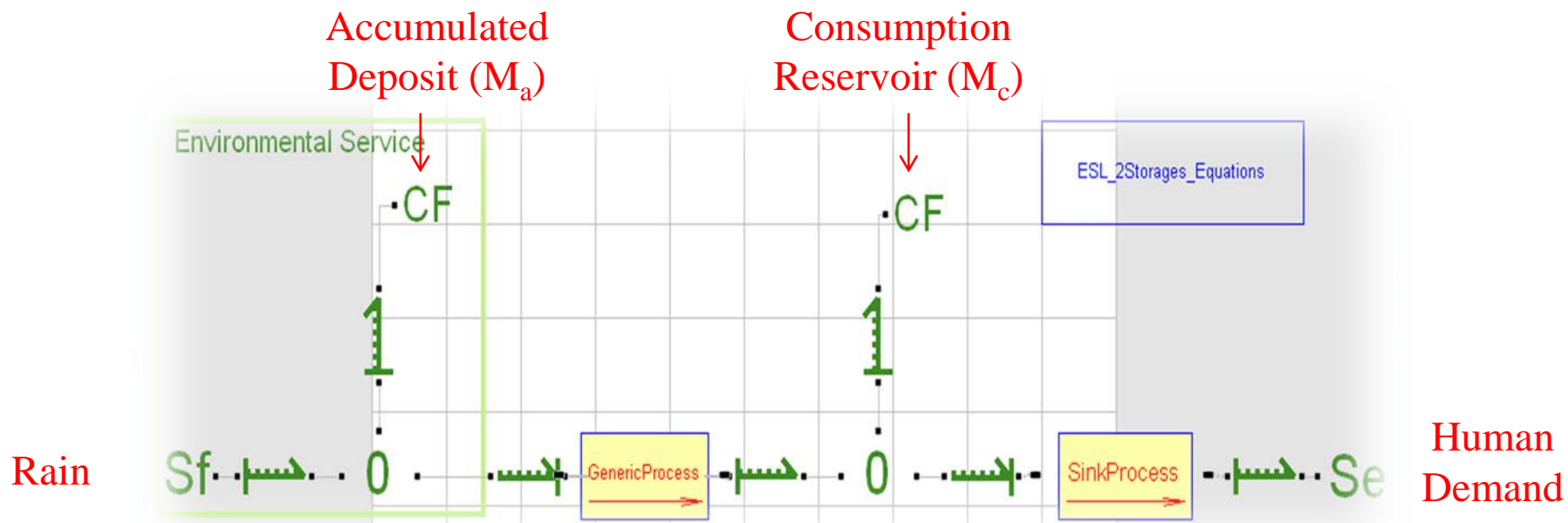
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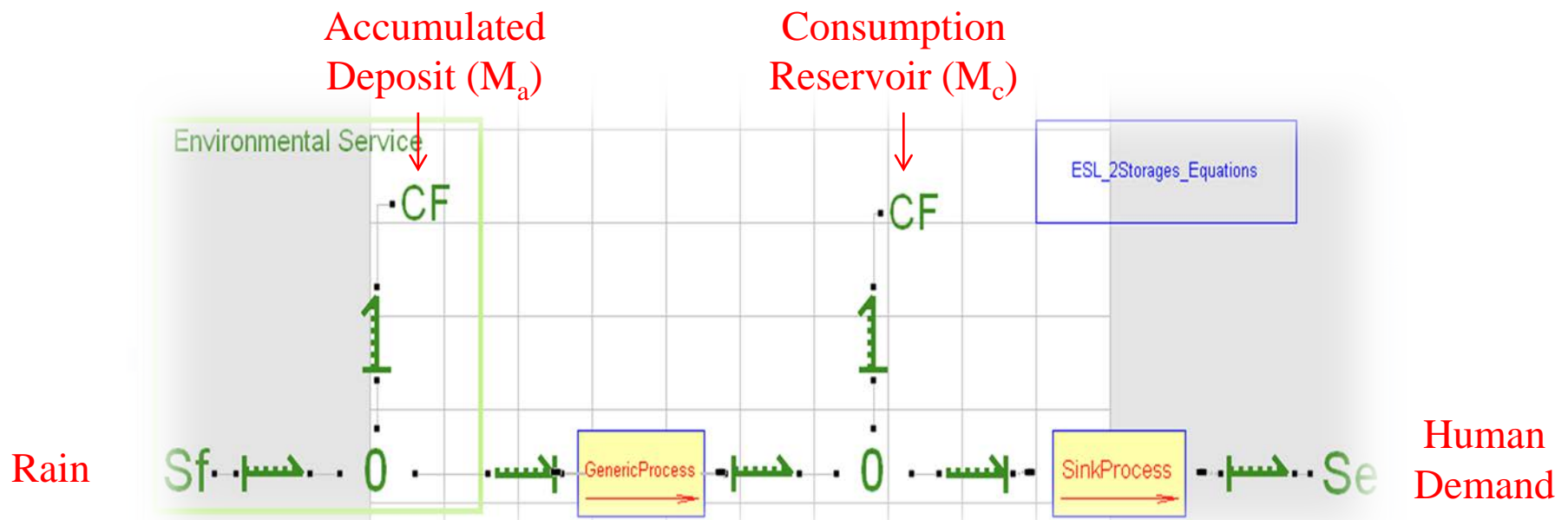
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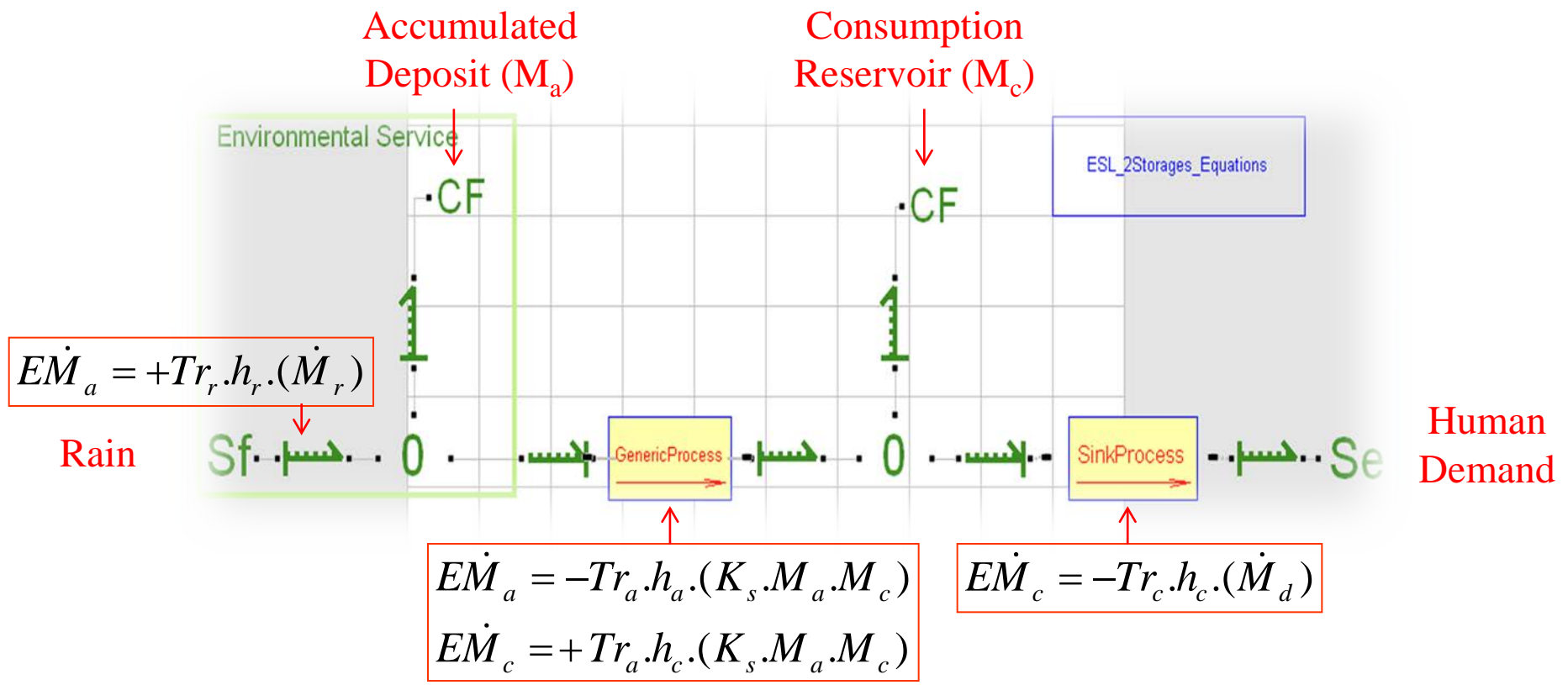
$$\begin{aligned}
 E\dot{M}_a &= Tr_r \cdot h_r \cdot (\dot{M}_r) - Tr_a \cdot h_a \cdot (K_s \cdot M_a \cdot M_c) \\
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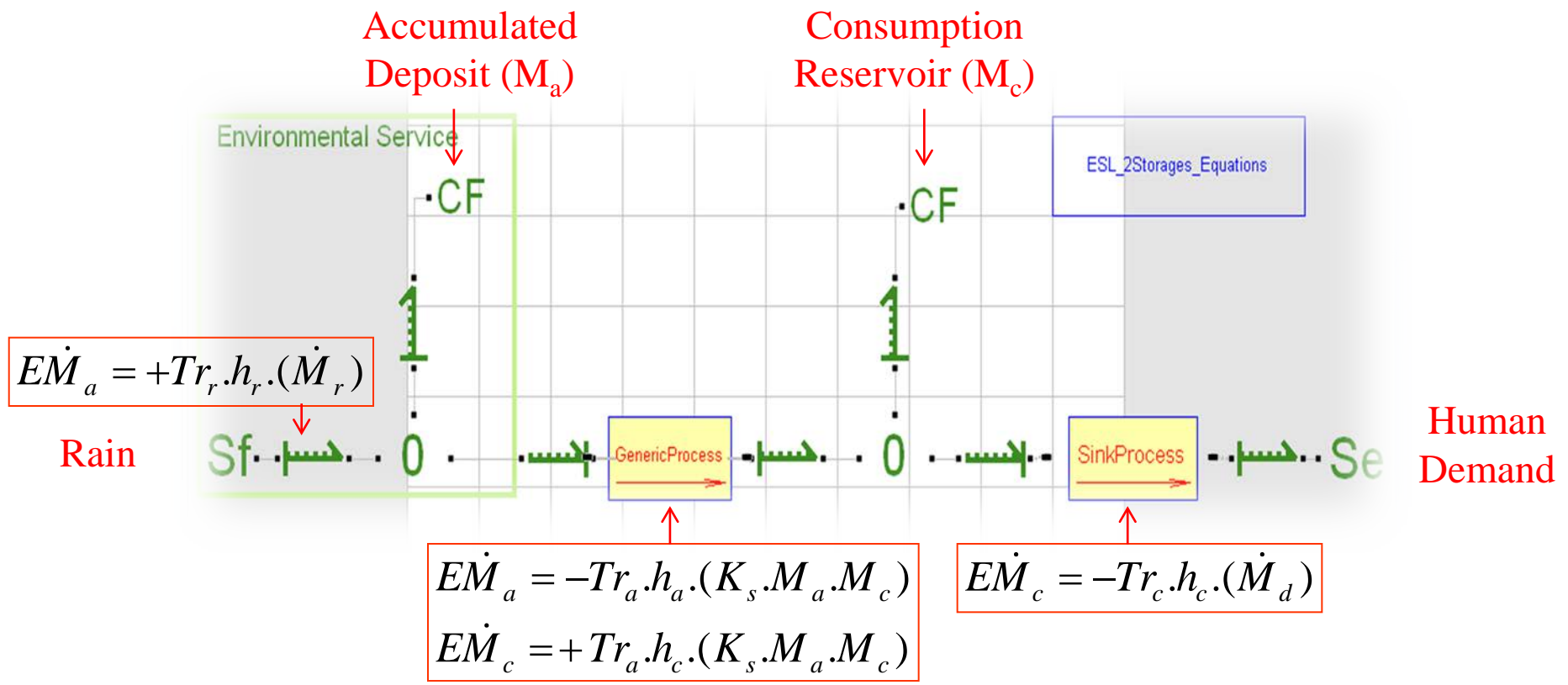
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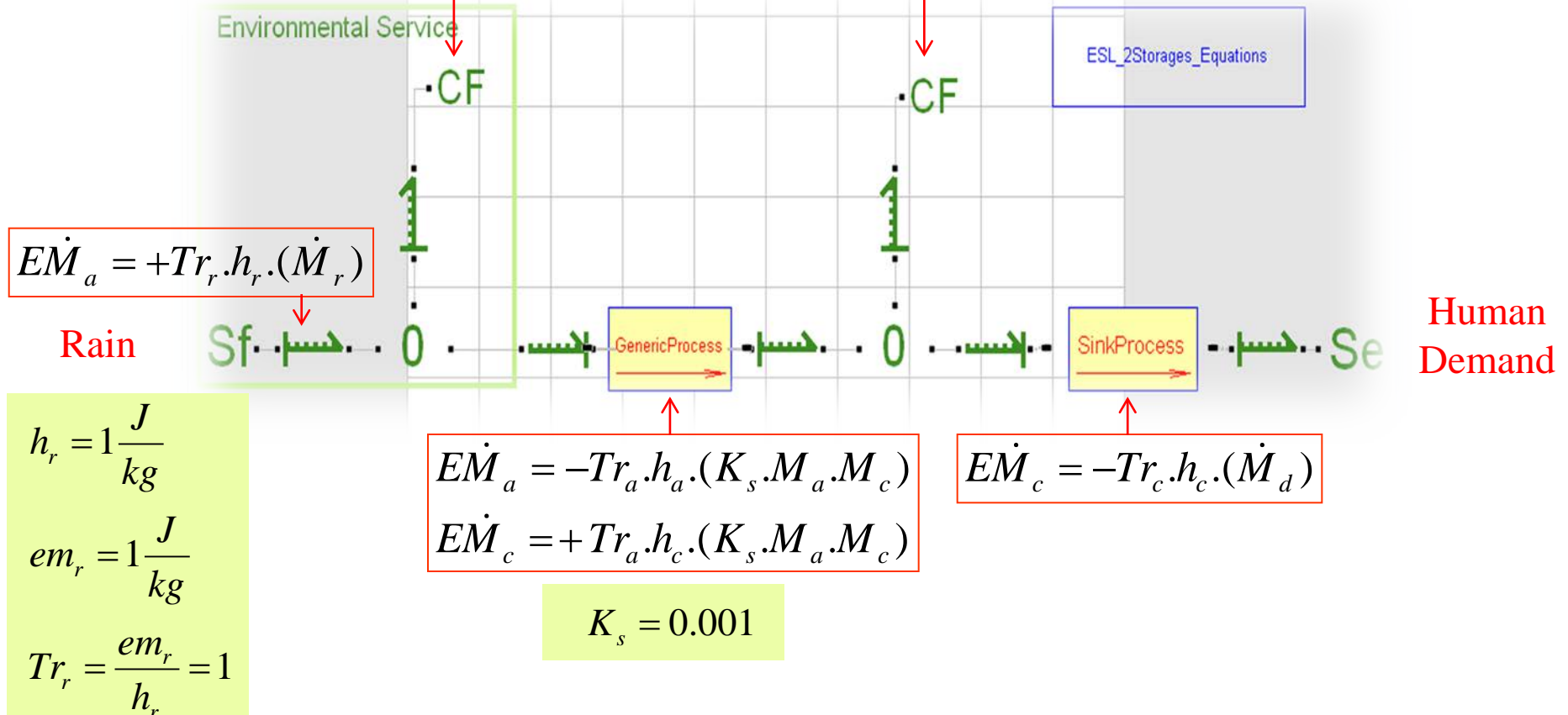
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$$h_a = 1 \frac{J}{kg}$$

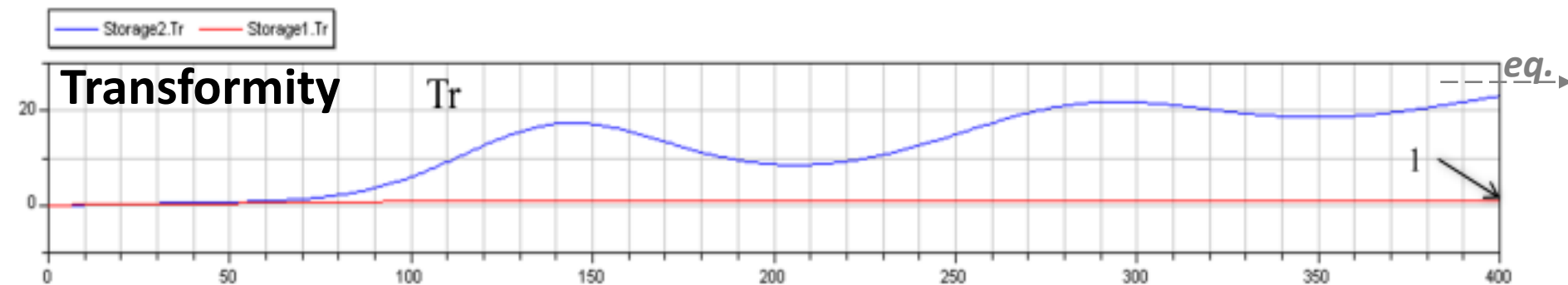
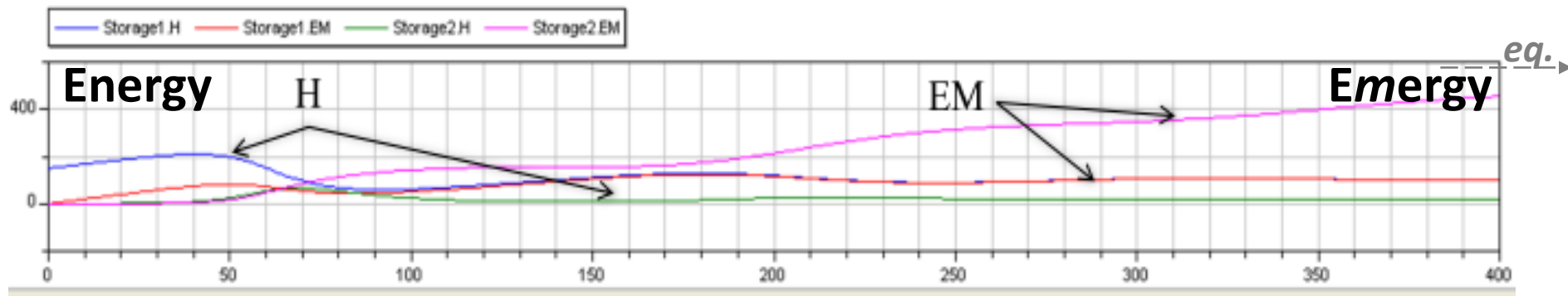
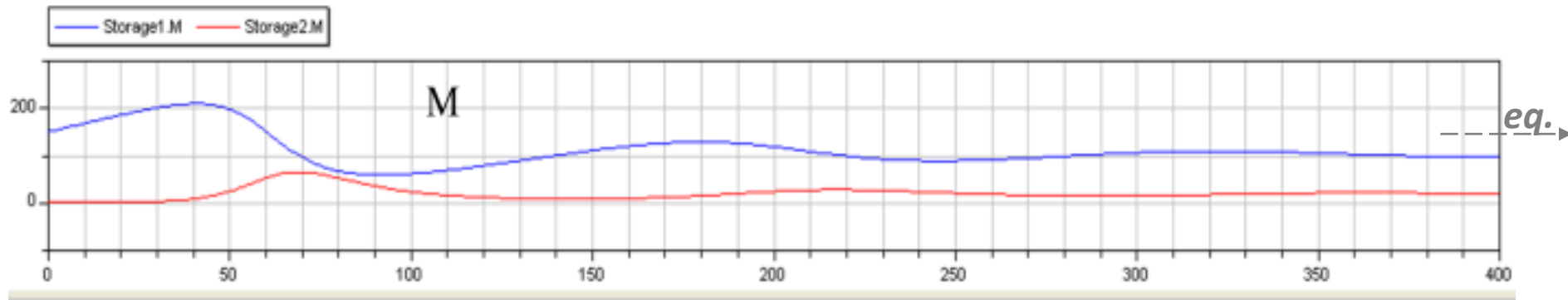
$$h_c = 1 \frac{J}{kg}$$

Accumulated Deposit (M_a)

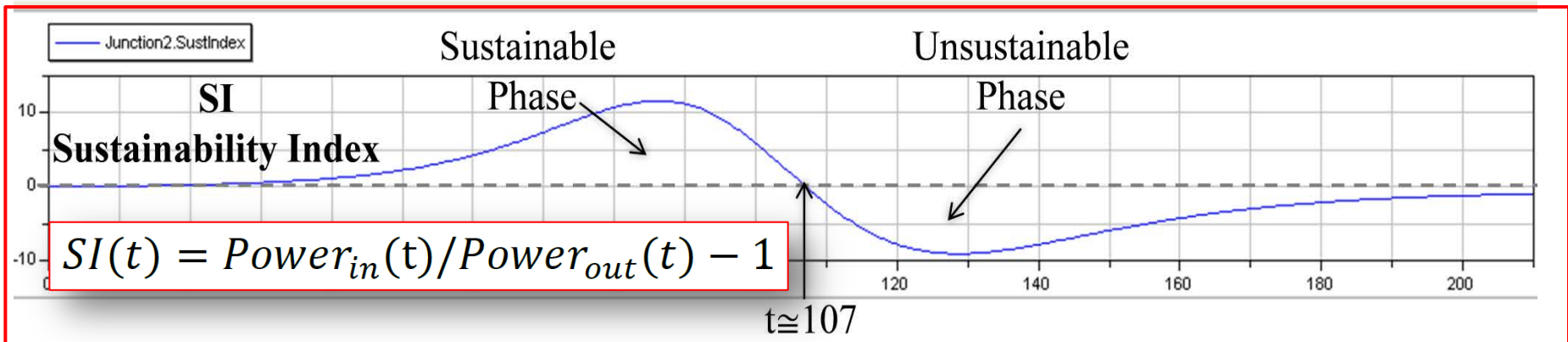
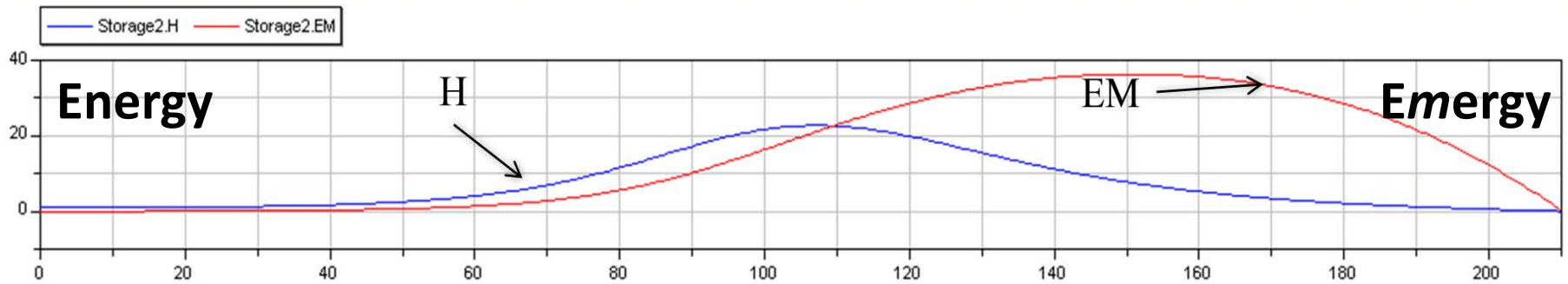
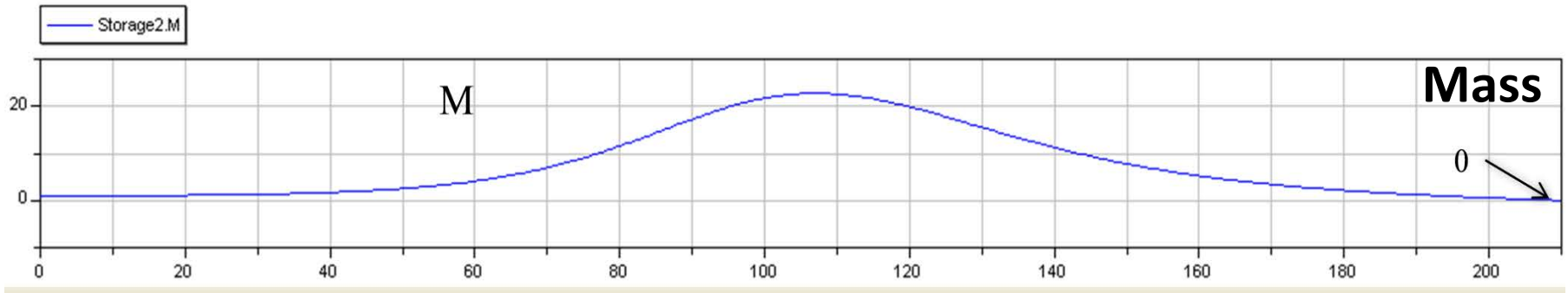
Consumption Reservoir (M_c)



- Accumulated quantities (**Deposit** and **Reservoir**)



- Experiment: Rain flow reduced 4x. Results for Reservoir.



- Eco Bond Graphs
 - A new “Plumbing Technology” for modeling Complex Dynamics Systems
 - A low-level tool to equip other higher-level modeling formalisms
 - with the ability to track *emergy* flows
- Hierarchical interconnection of EcoBG subsystems
 - Automatic and systematic evaluation of sustainability:
 - global tracking of *emergy* and
 - local checking of energy balances
- M&S practice
 - The laws of thermodynamics are **not an opinable** subject
 - Every sustainability-oriented effort should -at some point- consider *emergy*
- We should become able to **inform** both:
 - **decision makers** (experts, politicians, corporations) and
 - **people** who express their wishes (democratic societies)
 - about which are the **feasible** physical boundaries
 - within which their **-largely opinable-** desires and/or plans can be **possibly implemented in a sustainable fashion**.

Thanks for your attention !

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rcastro@dc.uba.ar

